

Inverse Problems for Philosophers

Bridging the gap between agent-based models and behavioral data

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University of Bochum, January 2025

- 1 Inverse problems for philosophers and agent-based modelers
- 2 A case-study of conventions: the metric signature in particle physics
 - How do physicists choose which convention to use in their own papers?
 - How do scientists resolve conflicting preferences in collaborations?
 - How do physicists' preferences get formed?

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- **Practical:** normative insights from models without connection to data may not be translatable into interventions/policies (abstract parameters in a computational model do not immediately connect to actionable parameters!)

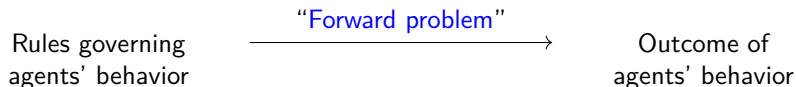
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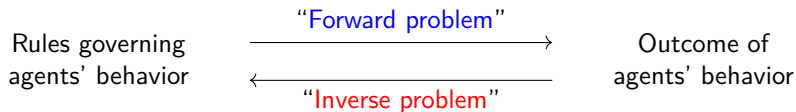
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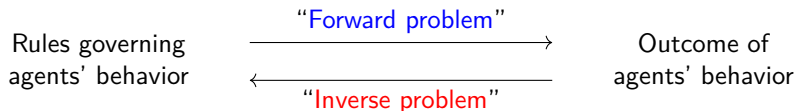
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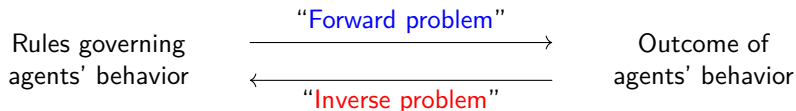
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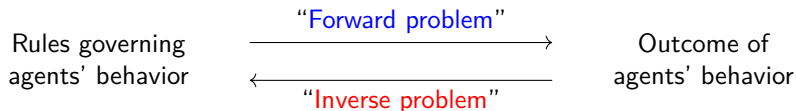
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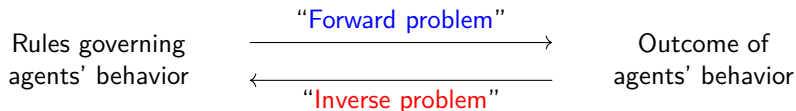
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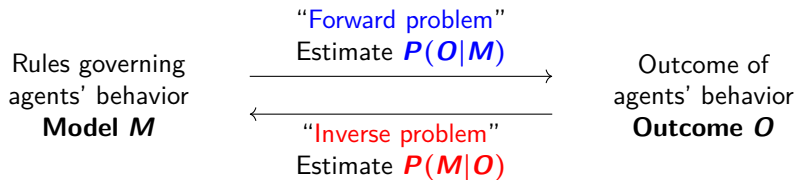
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 - 2 **Misspecification problems**: inverse problems may produce misleading results when modeling assumptions are "too wrong".
 - 3 **Computational problems**: solving inverse problems often involves intractable computations and requires approximation schemes.

Bayesian inference for inverse problems

- Both forward models and inverse problems have a stochastic/probabilistic component (random initialization, partially random decisions; uncertainty quantification...)
- We appeal to **probabilities** and **Bayesian inference**.



$$P(M|O) = \frac{P(O|M) \overbrace{P(M)}^{\text{Prior}}}{P(O)} \quad (1)$$

Model comparison and parameter estimation

$$P(M|O) = \frac{P(O|M) \overbrace{P(M)}^{\text{Prior}}}{P(O)} \quad (2)$$

$$P(\theta|O) = \frac{P(O|\theta) \overbrace{P(\theta)}^{\text{Prior}}}{P(O)} \quad (2)$$

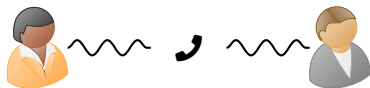
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Conventions

- **Coordination problems** arise when individuals would benefit from acting in a mutually compatible way, but it is somehow non-trivial to do so (Lewis, 1969).

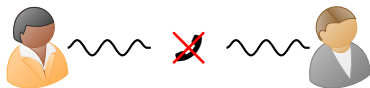


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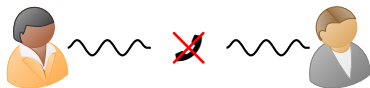
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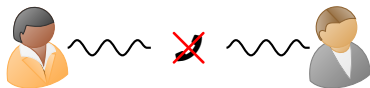


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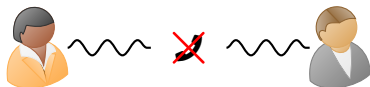
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 - Example: left-hand or right-hand traffic.
 - Language! “The syllable ‘big’ could have meant ‘small’ for all we care, and the red light could have meant ‘go’” (Quine, foreword to Lewis 1969)

Conventions in the literature

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Most often: idealized formal models or controlled experiments. Few studies in naturalistic settings!

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- Both choices are legitimate, as long as one remains consistent.

A heated debate



A heated debate

 **the finite physicist** @Fini
(-,+,+,+) metric signature

"Cook the pizza for $\sqrt{-1}$
deranged

14 26

Cliff Burgess @CbursesCliff · 10 août 2023
When her family finds you use the wrong **metric**...


Enez Özen @Enezator · 10 août 2023
Every pleasure in life has a price




0:00 / 0:32


4 4 32 3k


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 **Will Kinney** @WKCosmo · 12 oct. 2022
Be sure to check your kids' candy this year. Just found this **metric** inside a Snickers bar.



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Greg Trayling @GregTrayling · 27 avr. ...
Metric convention reveal parties for graduating physics majors, hear me out.

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Superconformal Hassaan
@Hassaan_PHY

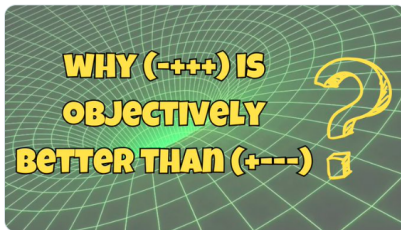
...

This is a small post to argue that $(-+++)$ metric is objectively better than the $(+--)$ metric. Before starting, let me mention that I studied QFT in the $(+---$) metric (from Peskin and Schroeder).

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[#Physics](#) [#scicomm](#)

[Traduire le post](#)



Greg Trayling @GregTrayling · Metric convention reveal part out.

1



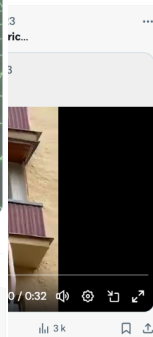
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Inverse problems and conventions

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 - 1 How do scientists decide which convention to use in a paper?
 - 2 How do they resolve conflicting preferences in collaborations?
 - 3 What factors shape scientists' preferences?

- Data collected from **Inspire HEP** (authorship/citation metadata) and **arXiv** (LaTeX source)
- Categories: hep-th (high-energy physics theory), hep-ph (phenomenology), gr-qc (gravitation and cosmology), astro-ph (astrophysics)
- 22 500 papers classified according to their metric signature (mostly plus or mostly minus) using regular expressions.

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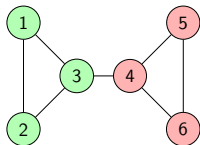
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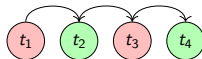
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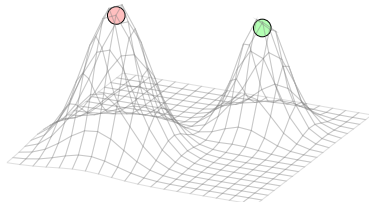
Social consistency
(coordination costs)



Individual consistency
(switching costs)



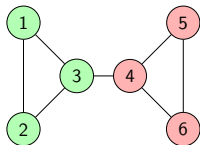
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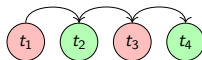
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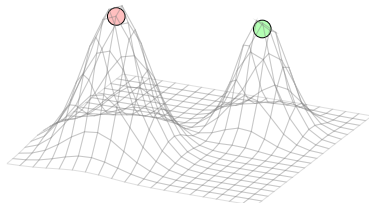
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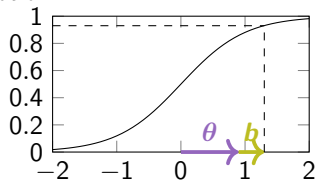


⇒ Are these involved in the context of the metric signature?


Individual and contextual consistency

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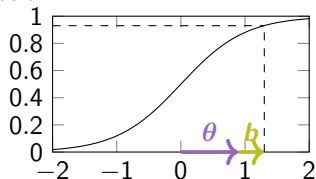
$$P(\sigma_d = +1 | \theta(\text{🧑}), b(c_d)) = f(\underbrace{\theta(\text{🧑})}_{\text{Author's preference}} + \underbrace{b(c_d)}_{\text{Effect of research area}})$$



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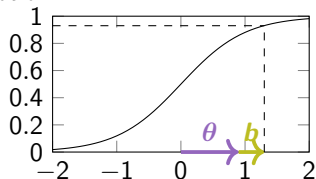


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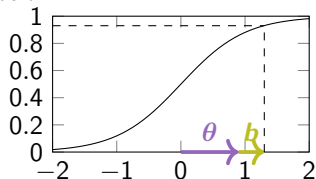


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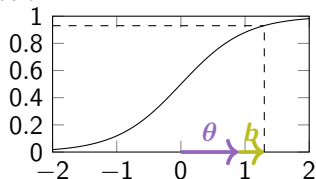


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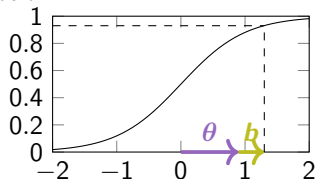


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- **Given physicists’ choices in their solo-authored papers, we can infer back θ and b using Bayesian inference.**

Individual and contextual consistency

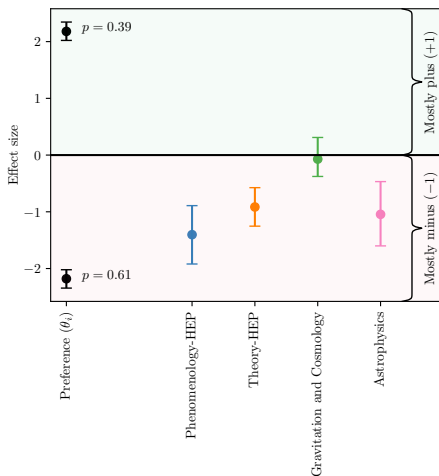


Figure: Individual consistency (preferences) matter the most, but adaptation to the context also occurs.

Individual and contextual consistency

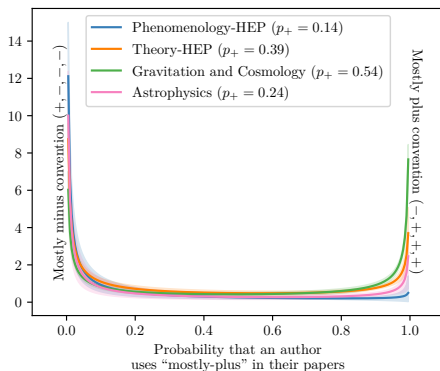


Figure: Physicists tend to always be using the same convention

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Inferring preference-aggregation mechanisms in conflicts

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 - Majoritarian strategy (the majority preference prevails)

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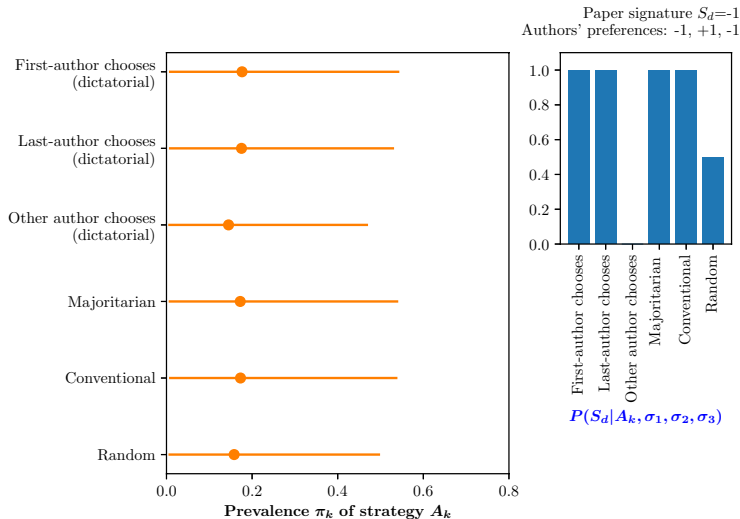
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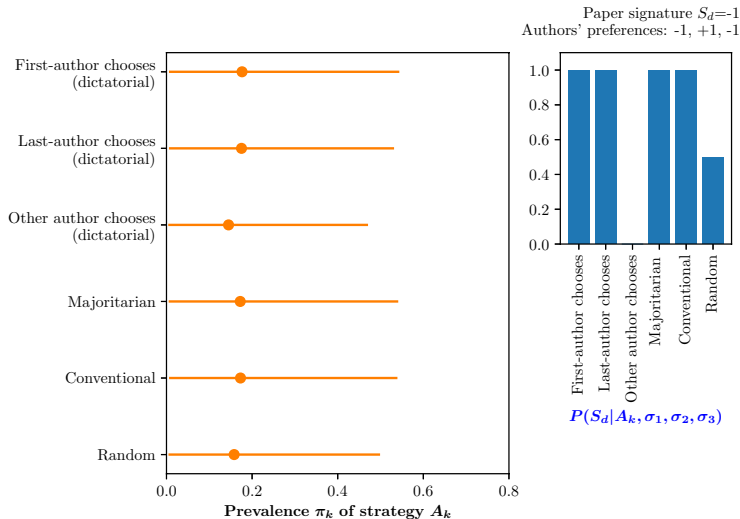
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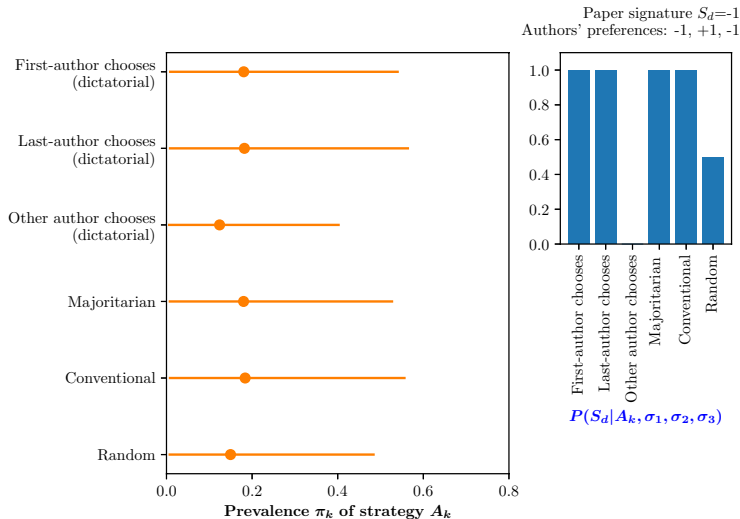
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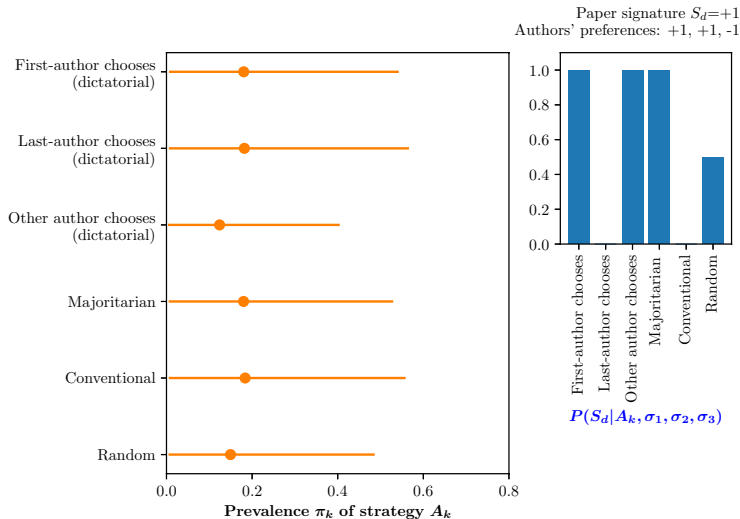
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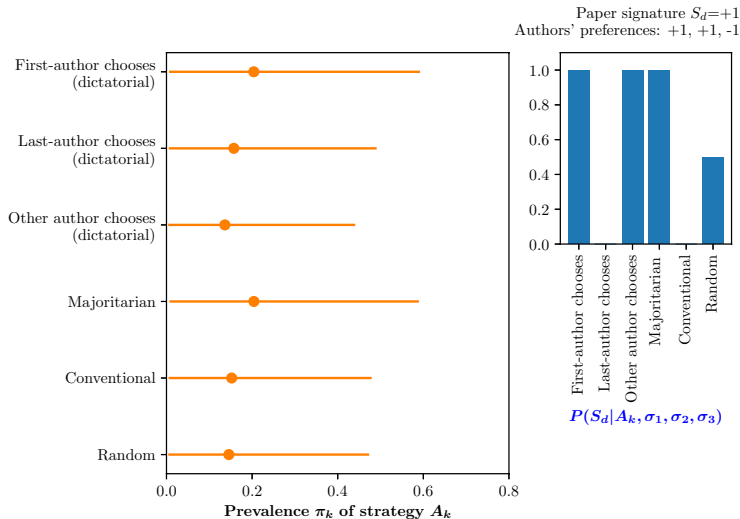
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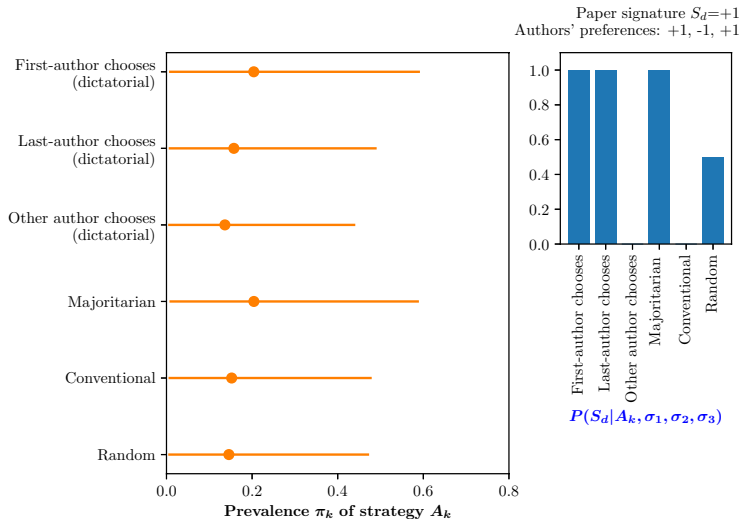
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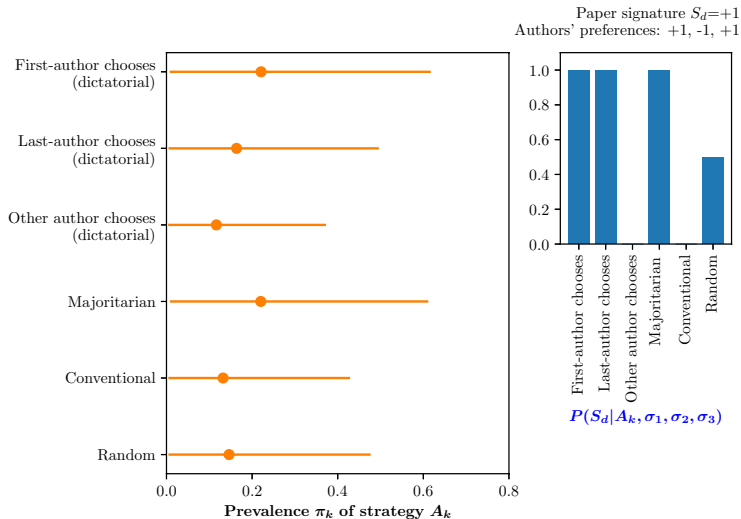
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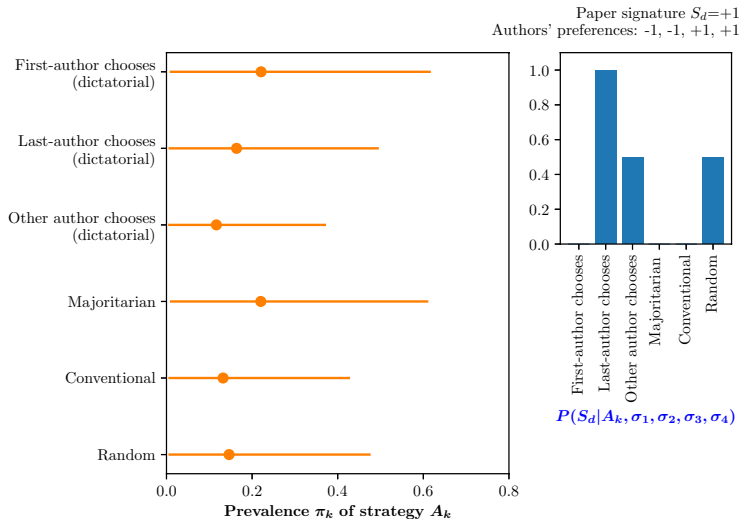
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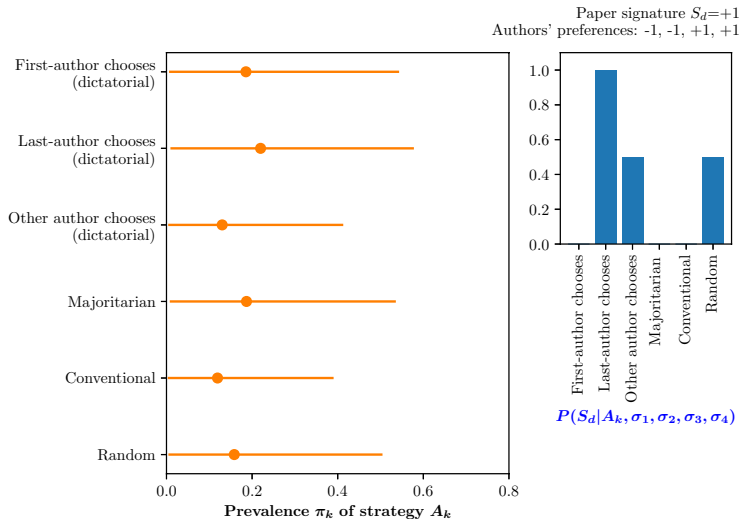
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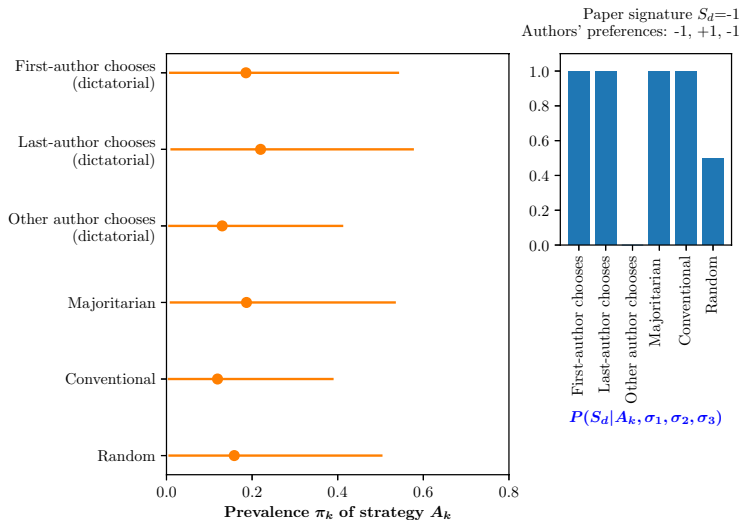
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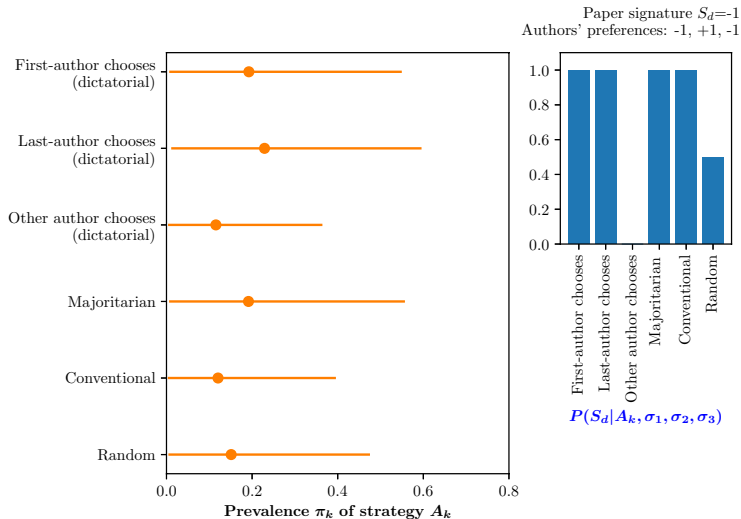
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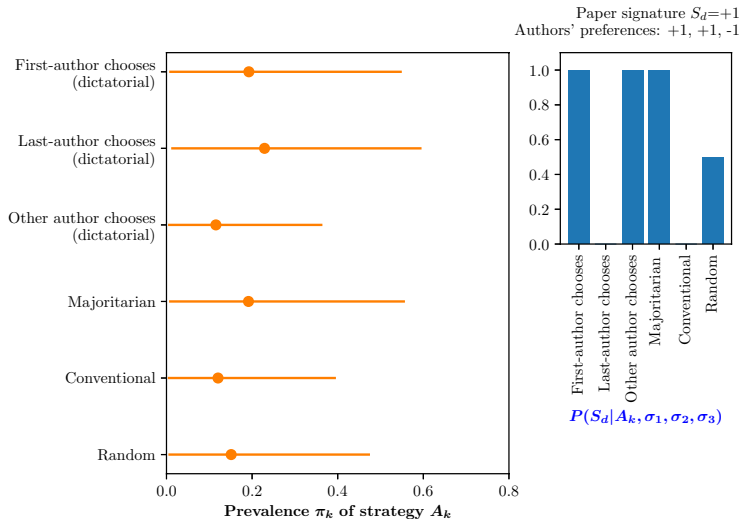
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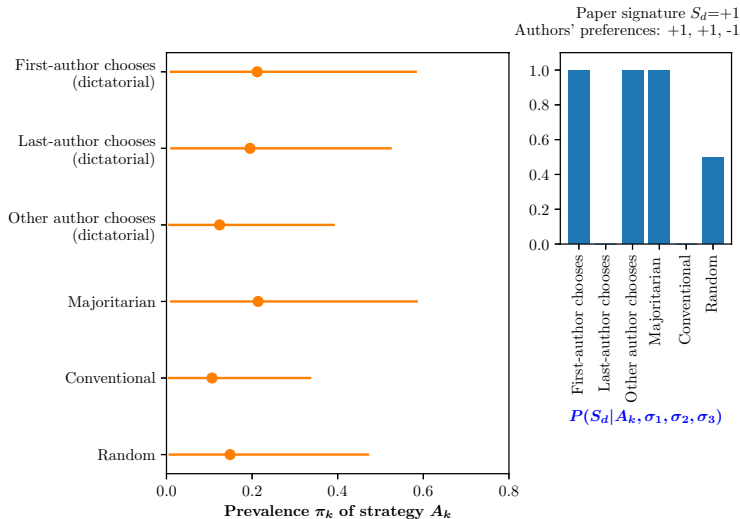
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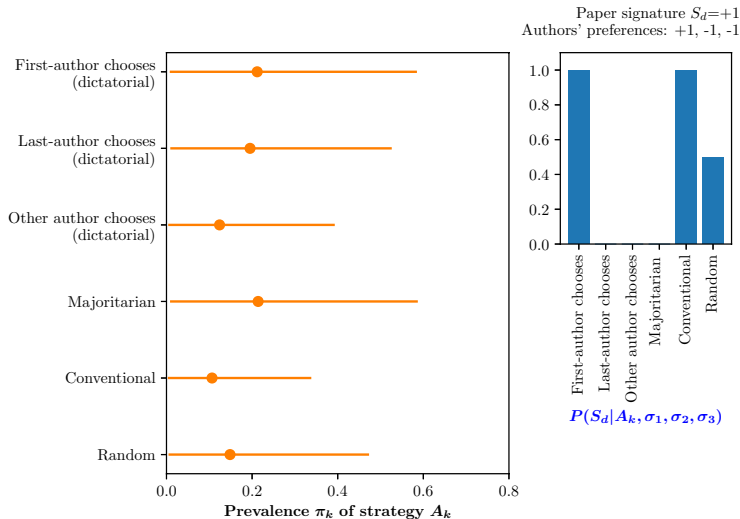
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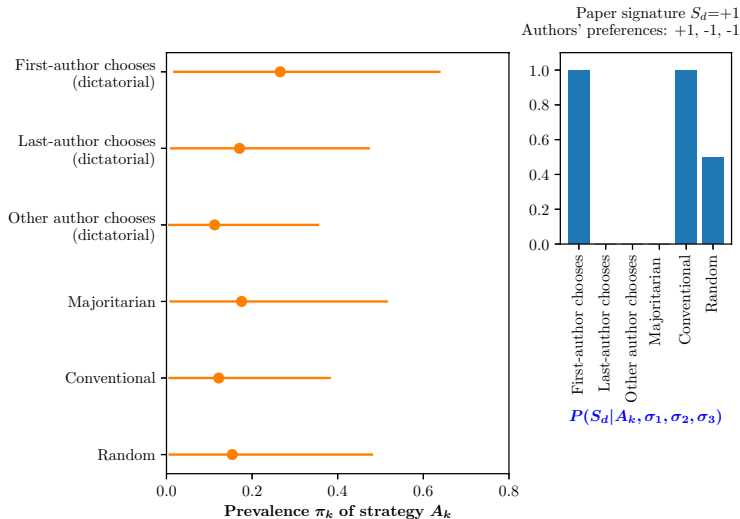
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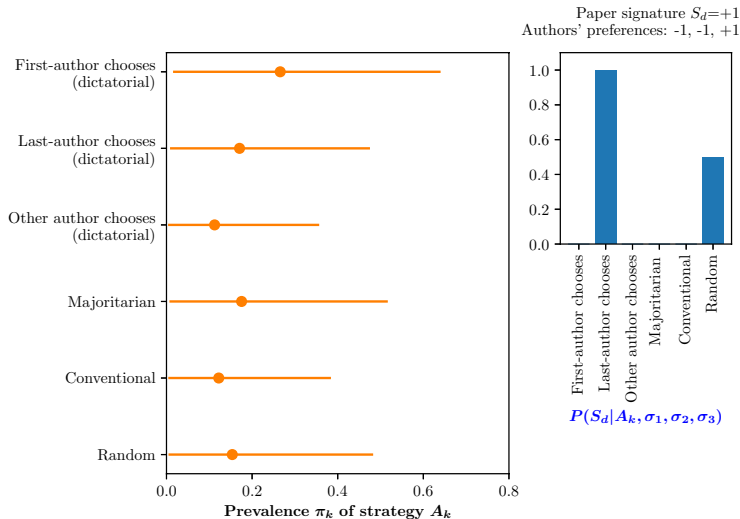
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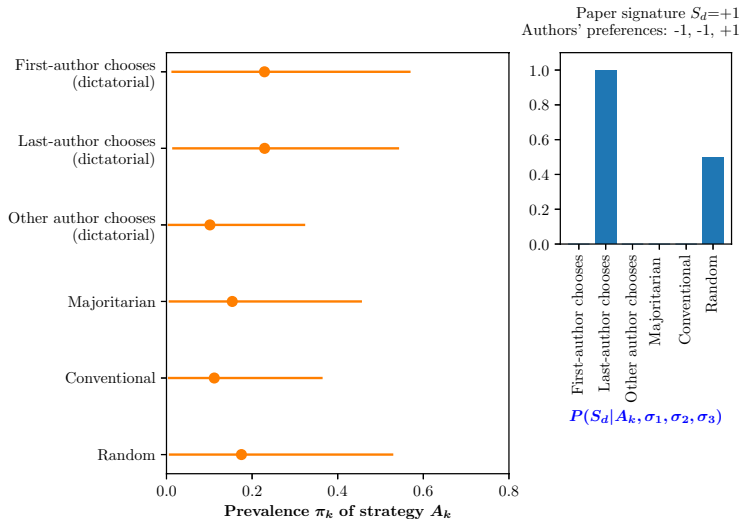
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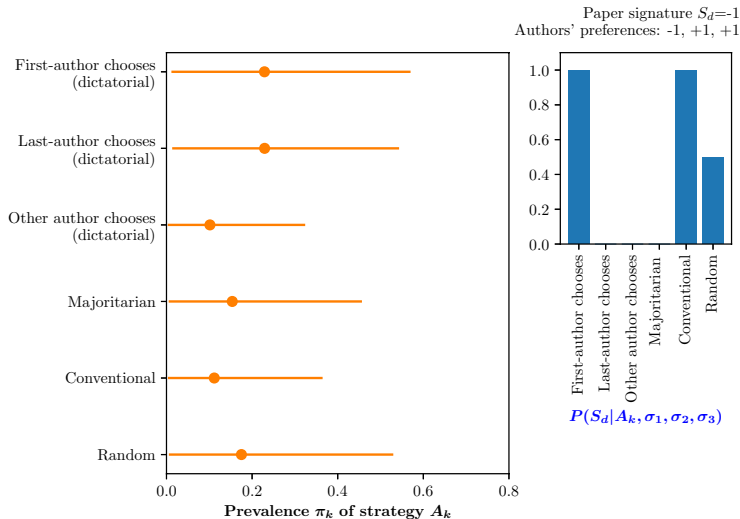
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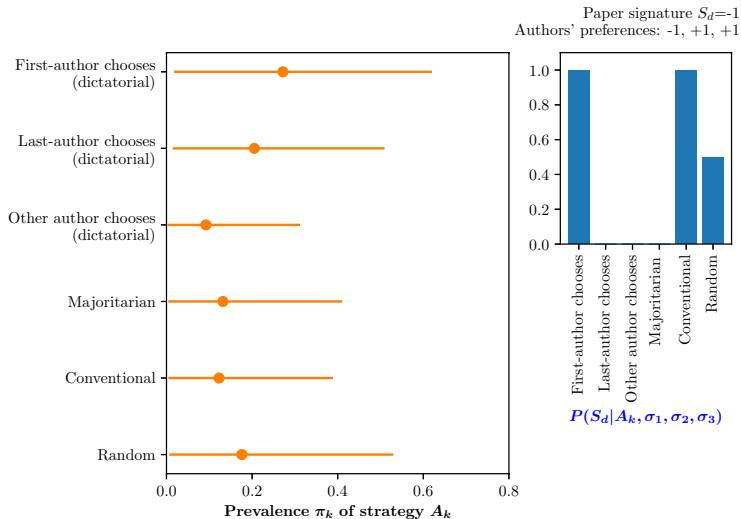
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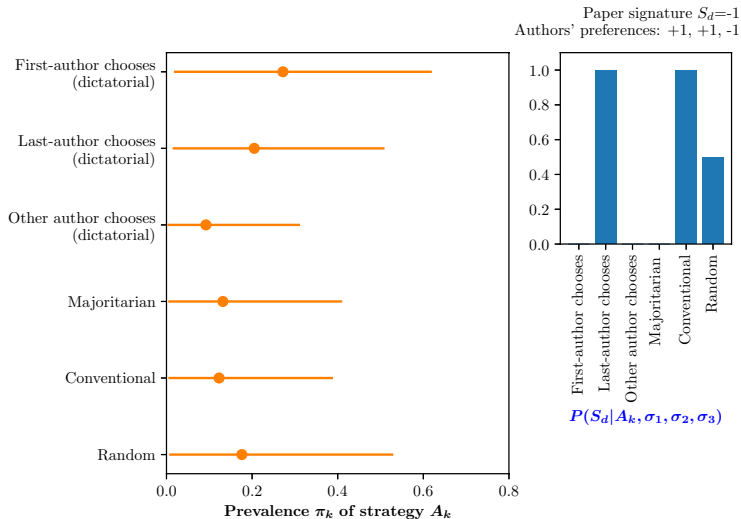
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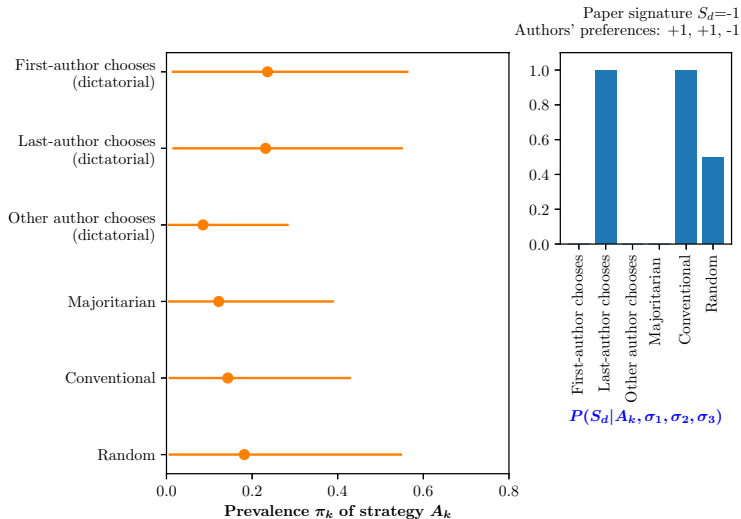
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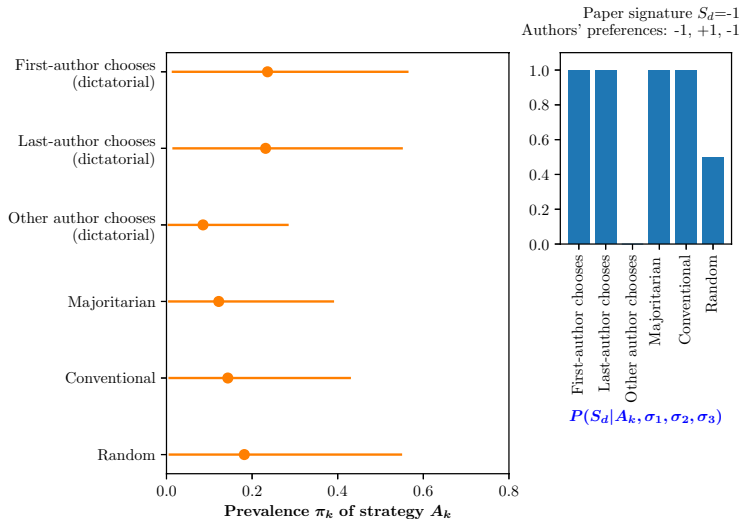
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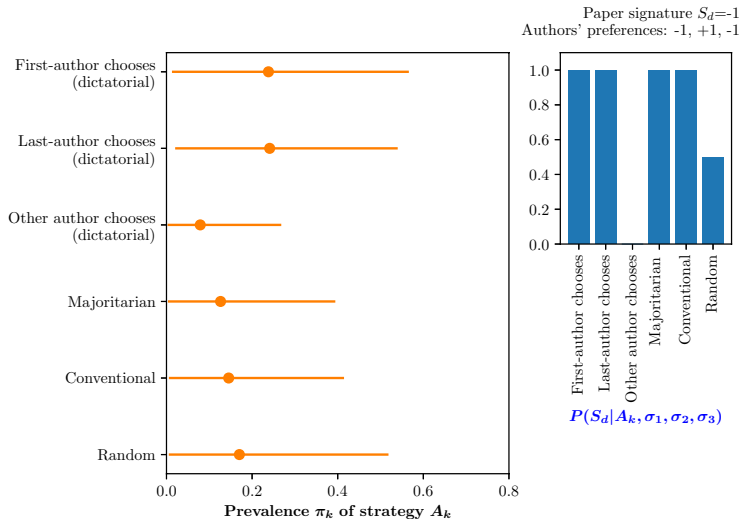
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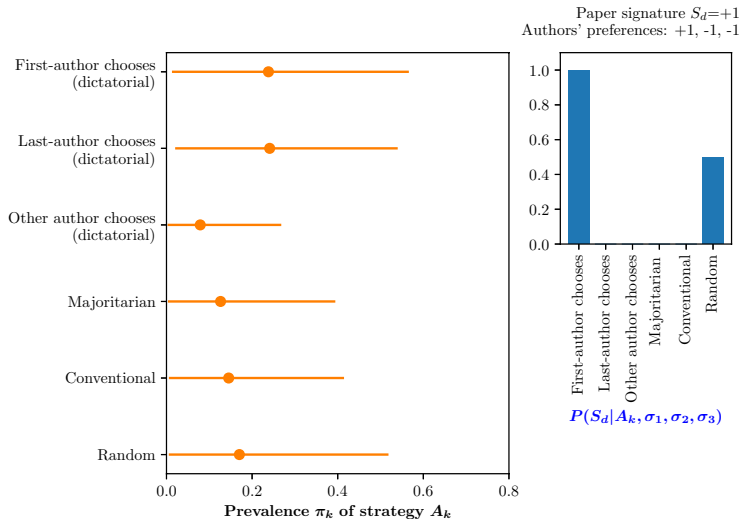
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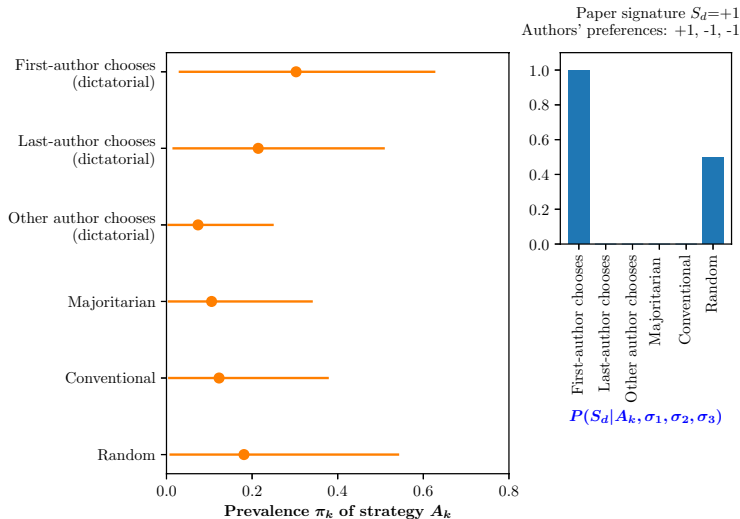
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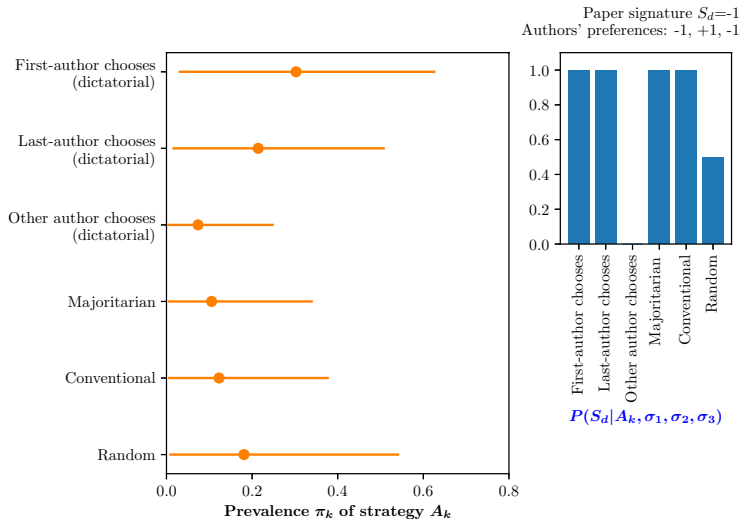
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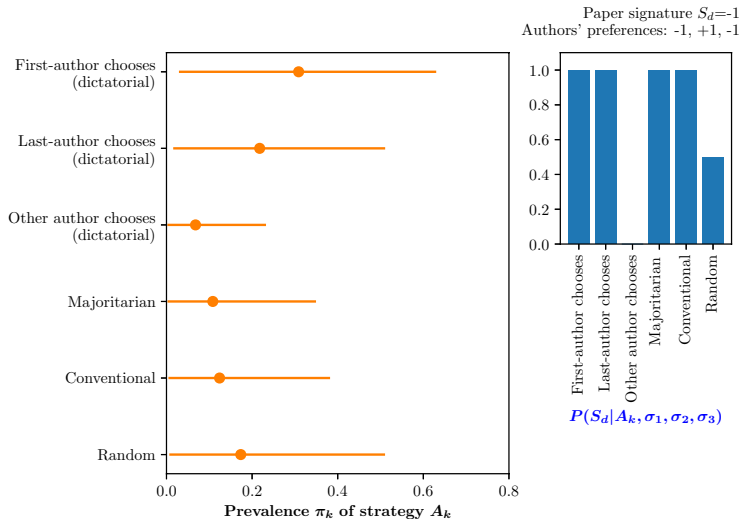
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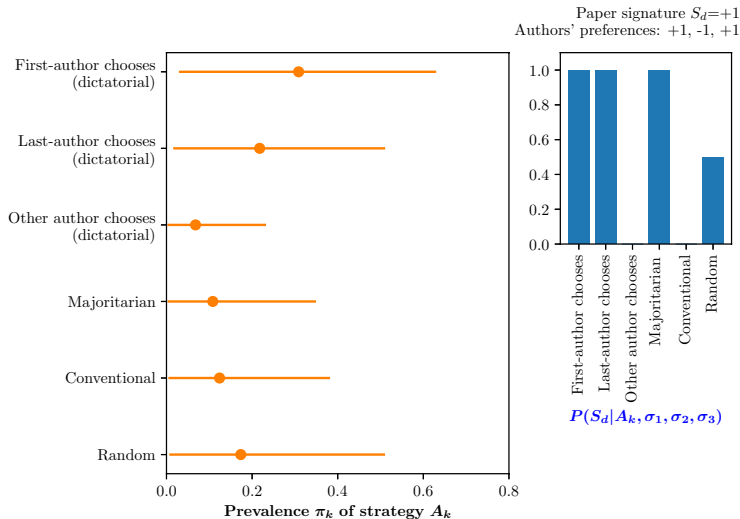
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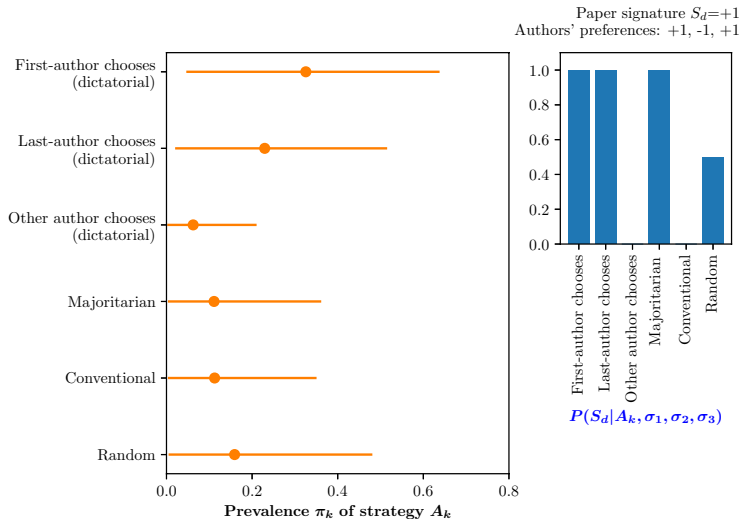
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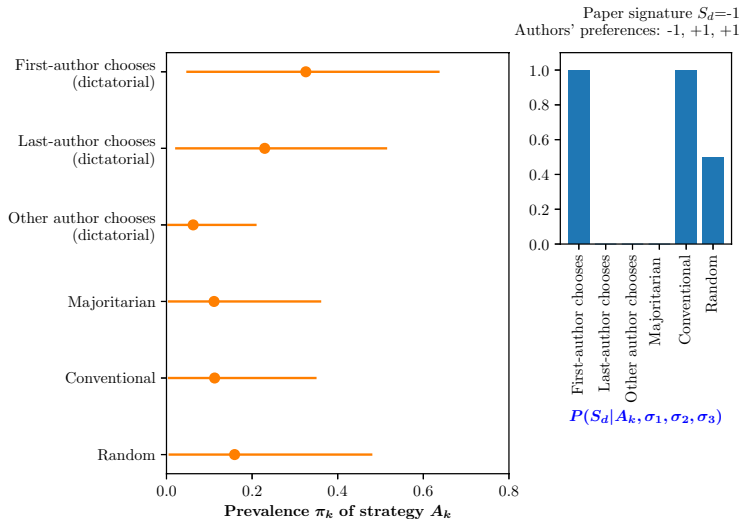
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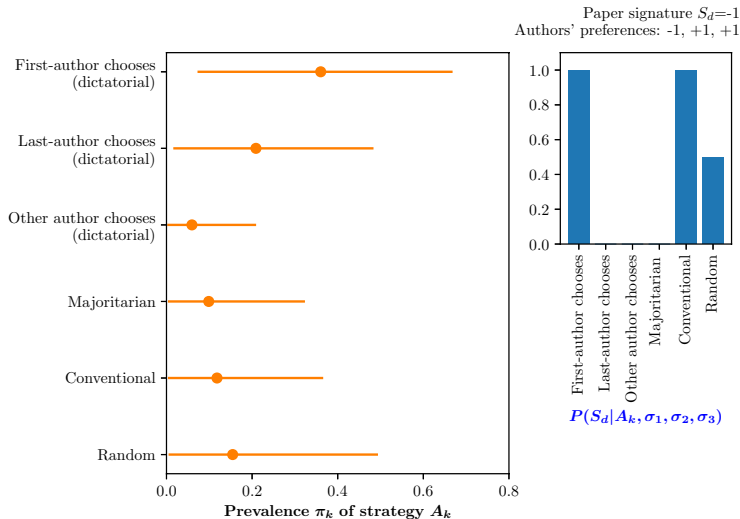
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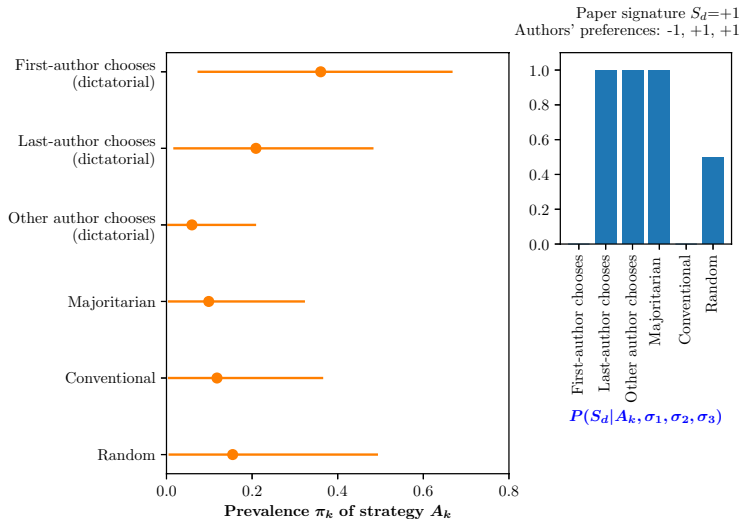
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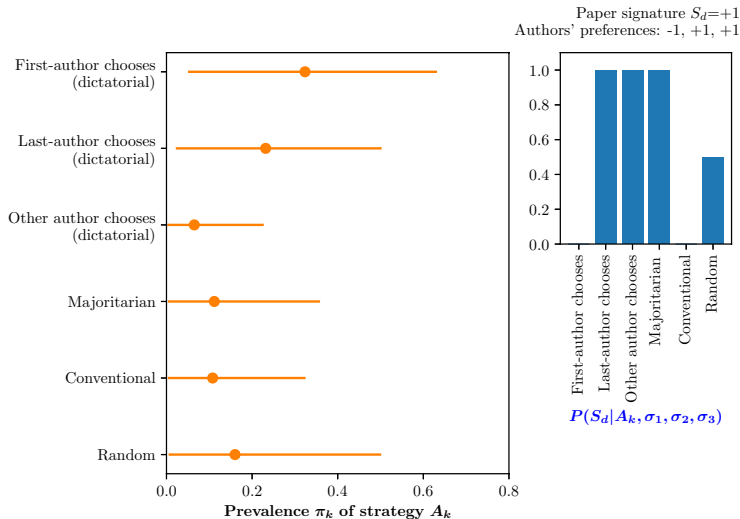
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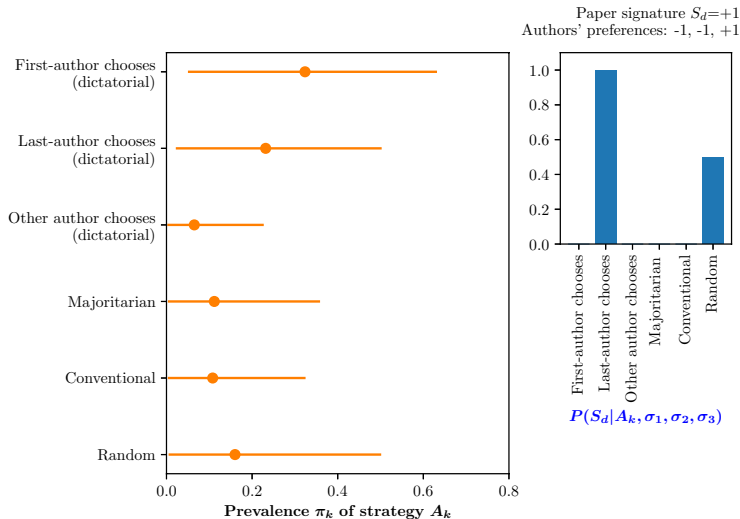
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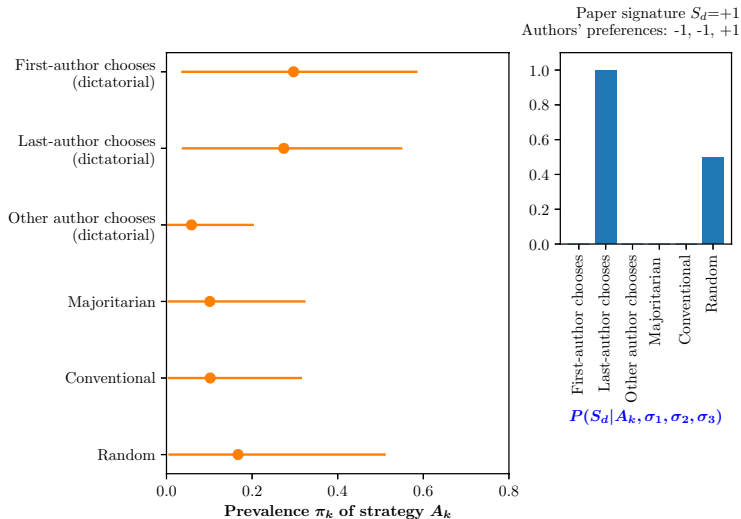
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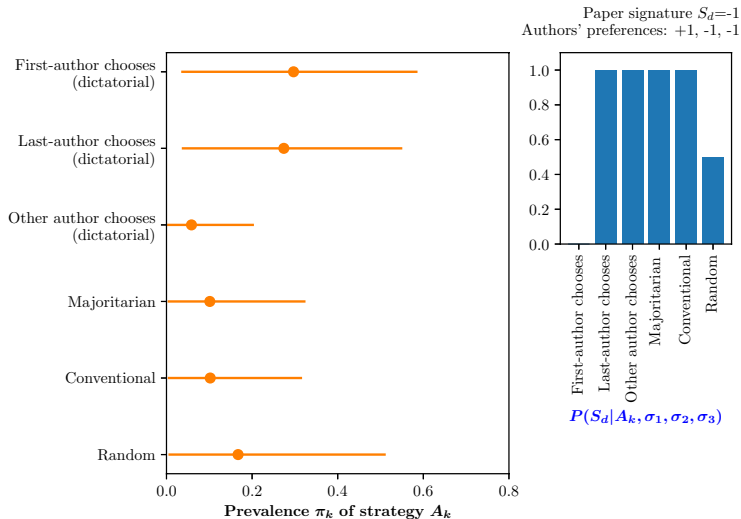
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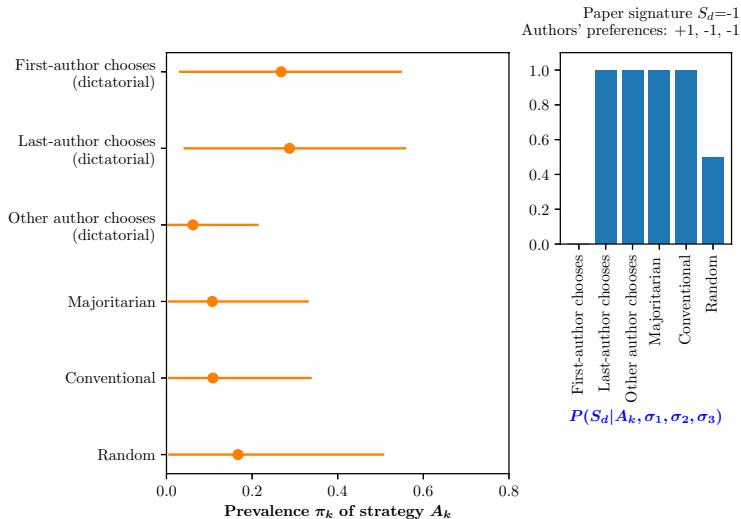
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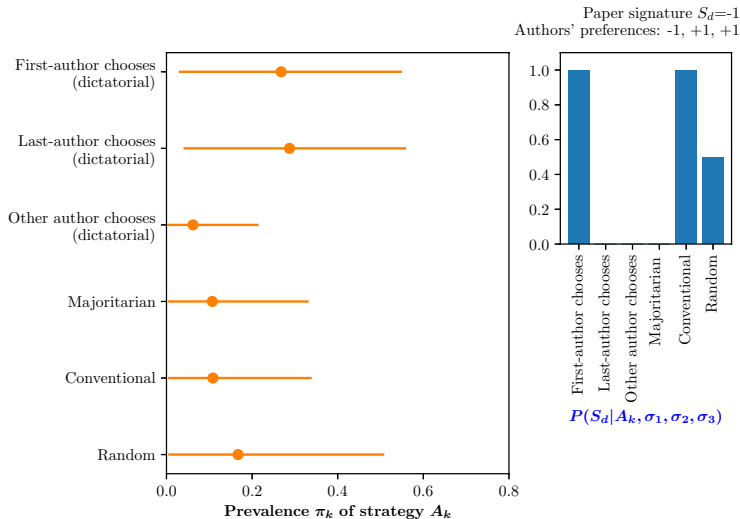
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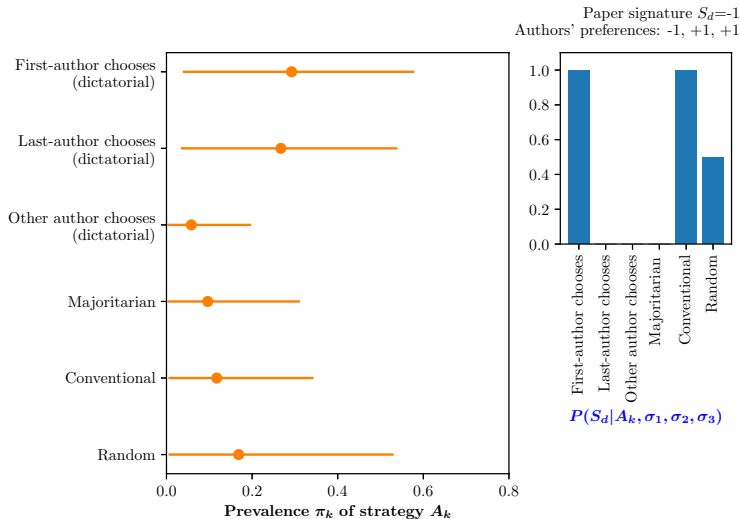
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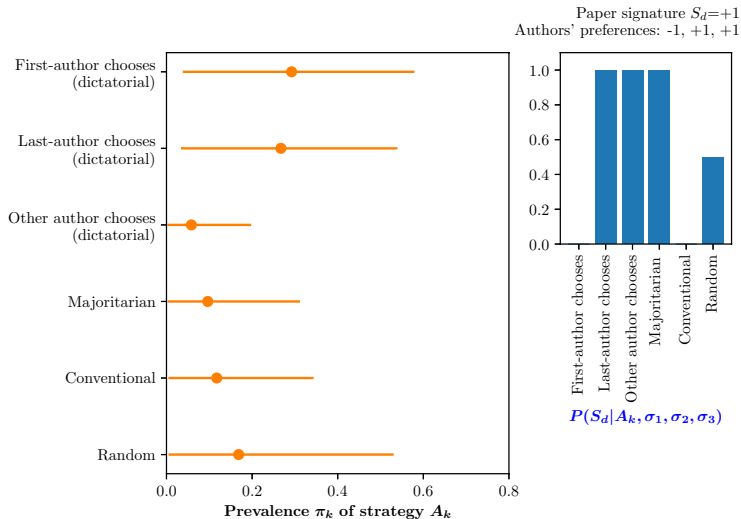
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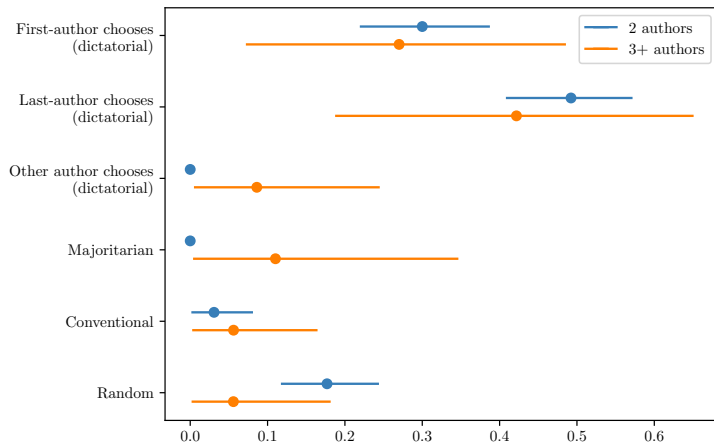


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Prevalence of each preference-aggregation strategy

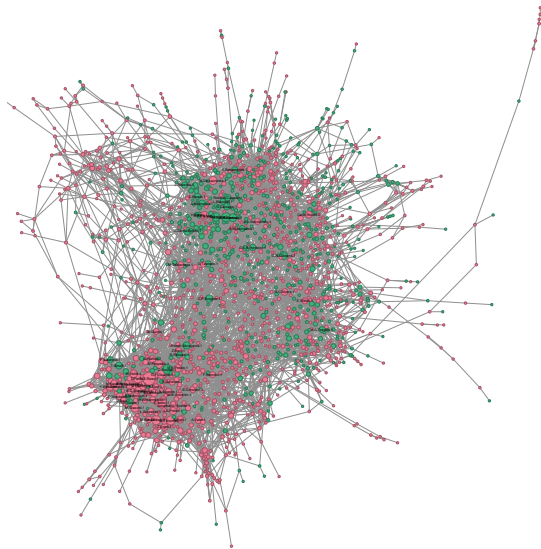


1 Inverse problems for philosophers and agent-based modelers

2 A case-study of conventions: the metric signature in particle physics

- How do physicists choose which convention to use in their own papers?
- How do scientists resolve conflicting preferences in collaborations?
- How do physicists' preferences get formed?

Authors' preferences



Observed outcome: the preference of each author,

$$O_{\text{obs}} = (\sigma_1, \dots, \sigma_n), \sigma \in \{-1, +1\}$$

($n = 2277$ authors)

How do physicists' preferences get formed?

- Let's assume three models of the formation of physicists' preference towards the convention:
 - 1 A “**strategic agent**” model (M_1) assuming that individuals navigate three costs (coordination costs, inconsistency costs, and maladaptation costs) depending on their collaborators' preferences and the research areas in which they publish.
 - 2 A **global cultural transmission model** (M_2), in which physicists settle once and for all for a specific convention with a certain probability that depends on their primary research area (textbooks?)
 - 3 A **local cultural transmission model** (M_3), in which physicists copy the preference of their first collaborator.
- Which of these is more plausible given the observed patterns of preferences?

Example: the strategic agent model (M_1)

The model M_1 has multiple unknown parameters:

- c_s : the cost of switching from one convention to another
- c_c : the cost of disagreeing with co-authors
- c_r the cost of using a suboptimal convention in a given research area

The **outcome** O_{sim} is the joint value of each author's preference:

$$O_{\text{sim}} = (\sigma_1, \dots, \sigma_n) \text{ where } \sigma_i = \pm 1$$

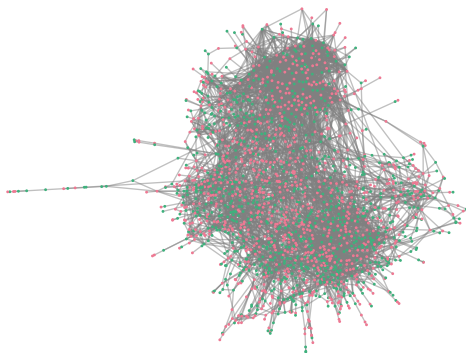
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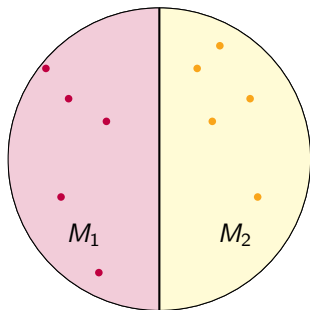


$$P(M_1|O) = \overbrace{P(O|M_1)} \frac{P(M_1)}{P(O)} \quad (4)$$

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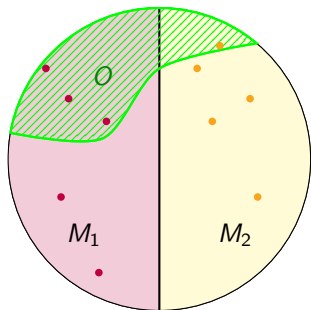
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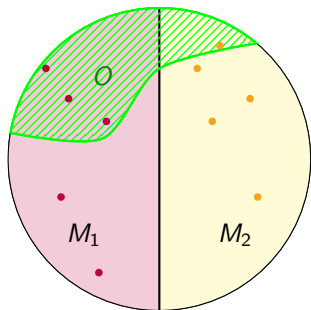
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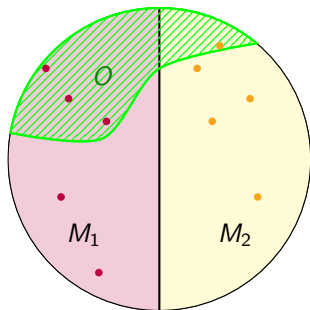
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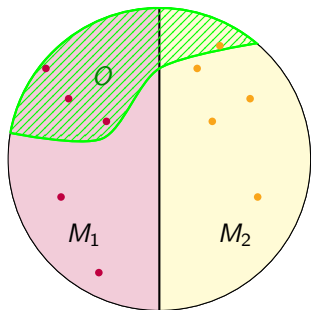


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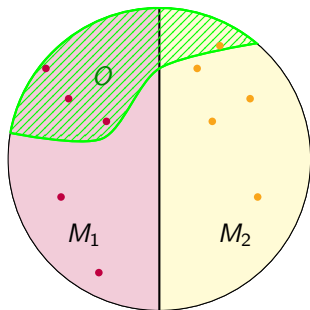
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$$P(M_1|O) = P(O|M_1) \frac{P(M_1)}{P(O)} = \frac{\begin{matrix} \text{3 green squares} & \text{1 pink square} \\ \text{1 pink square} & \text{3 green squares} \end{matrix}}{\begin{matrix} \text{3 green squares} \\ \text{3 green squares} \end{matrix}} = \frac{\text{3 green squares}}{\text{3 green squares}}$$

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Curse of dimensionality in simulation-based inference

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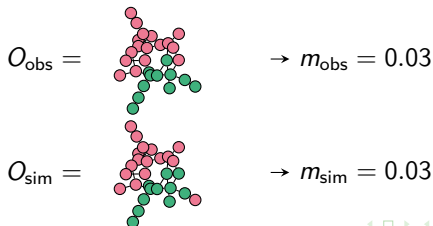
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$O_{\text{obs}} =$  $\rightarrow m_{\text{obs}} = 0.03$

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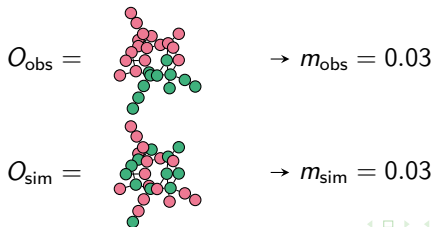
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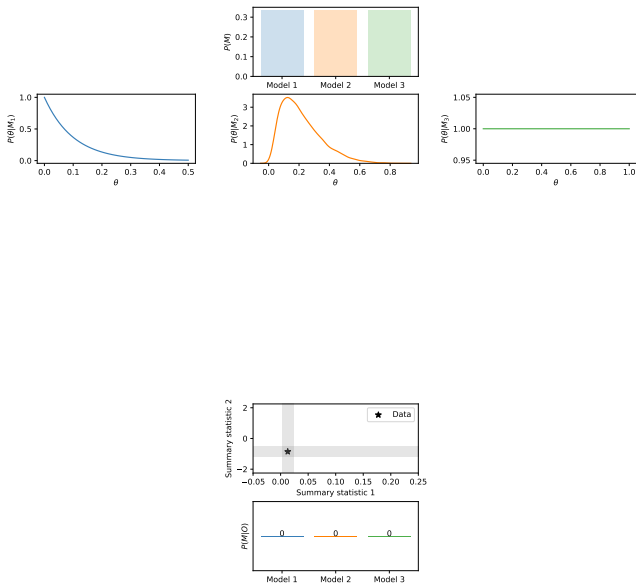


Summary statistics in simulation-based inference

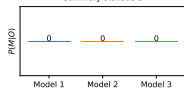
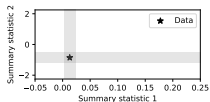
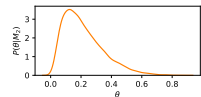
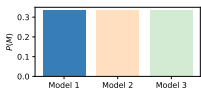
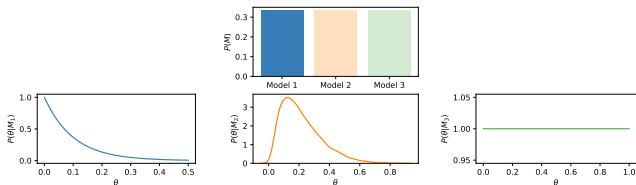
There are two main approaches for choosing adequate summary statistics:

- 1 Hand-picking interpretable summary statistics based on our own intuitions.
- 2 Using sophisticated methods to learn statistically optimal (but potentially un-interpretable) summary statistics. Optimal summary statistics reduce our posterior uncertainty given a fixed amount of data.

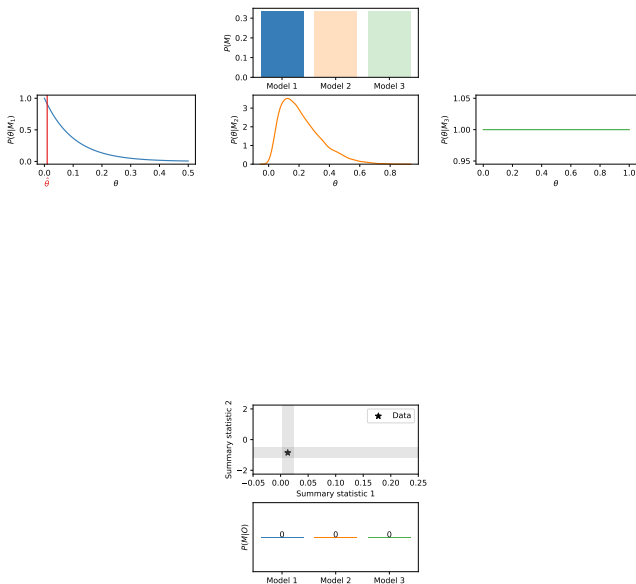
Simulation-based inference with summary statistics



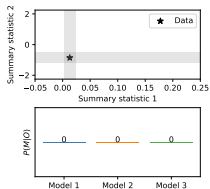
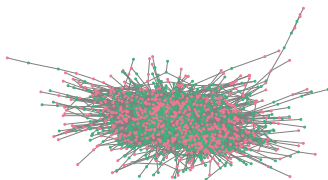
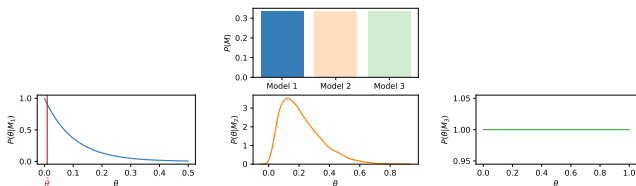
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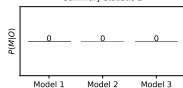
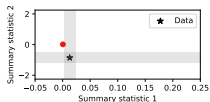
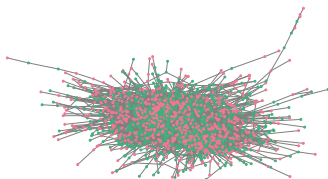
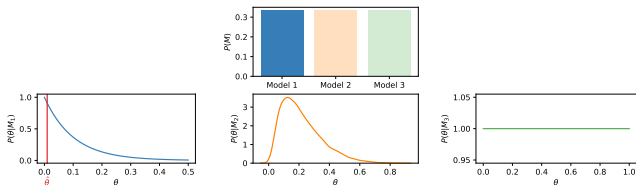
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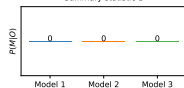
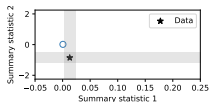
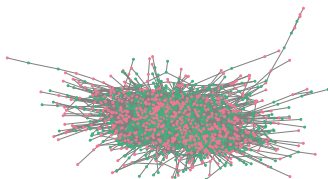
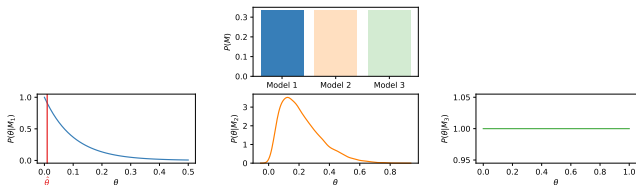
Simulation-based inference with summary statistics



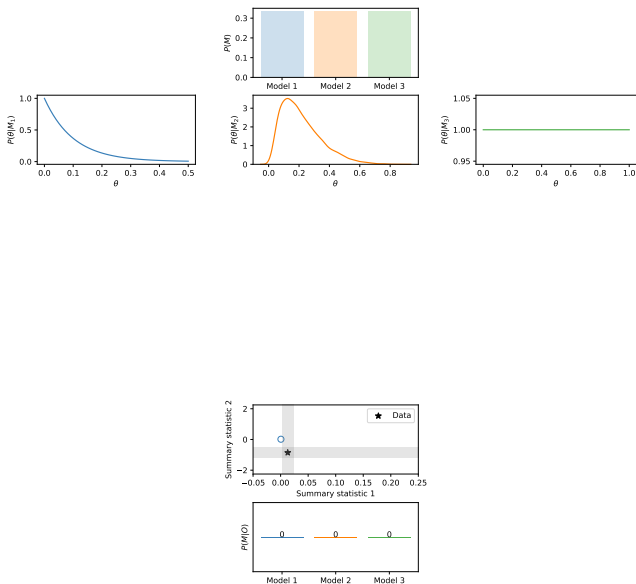
Simulation-based inference with summary statistics



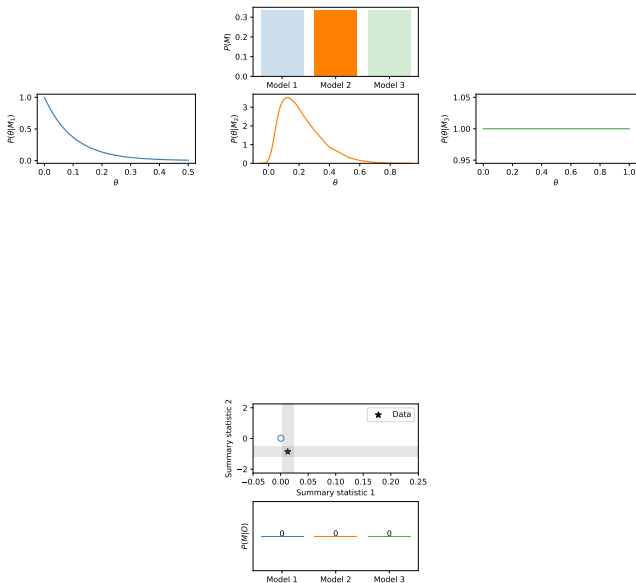
Simulation-based inference with summary statistics



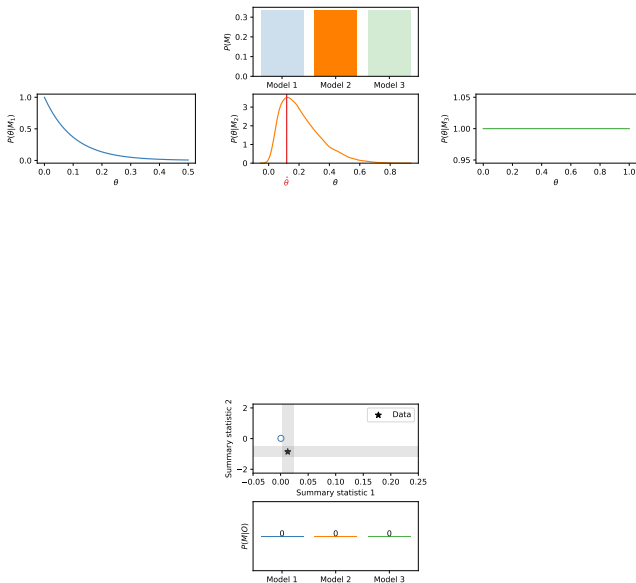
Simulation-based inference with summary statistics



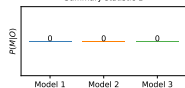
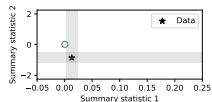
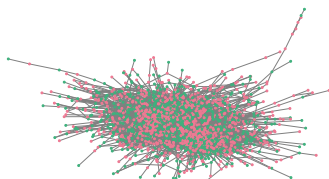
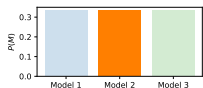
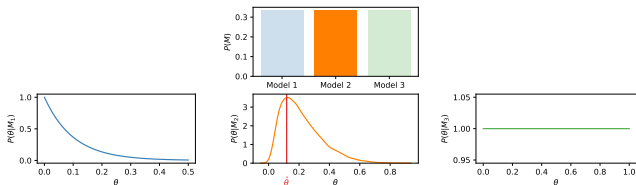
Simulation-based inference with summary statistics



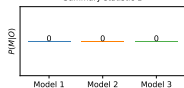
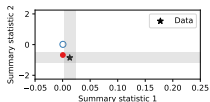
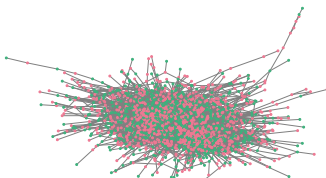
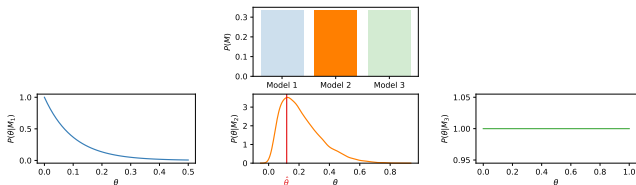
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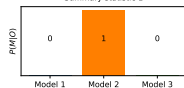
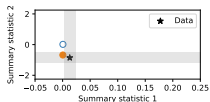
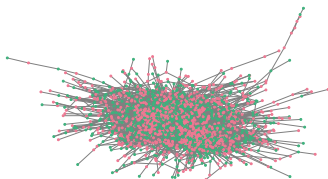
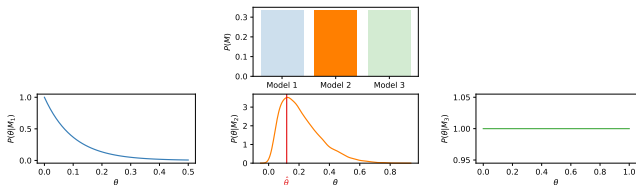
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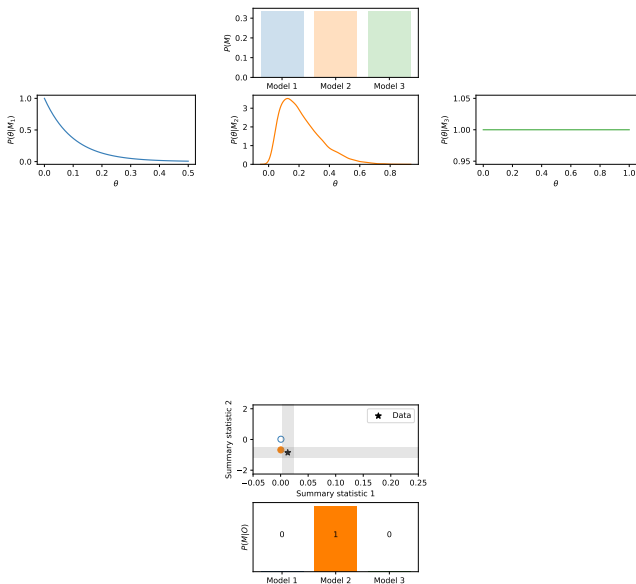
Simulation-based inference with summary statistics



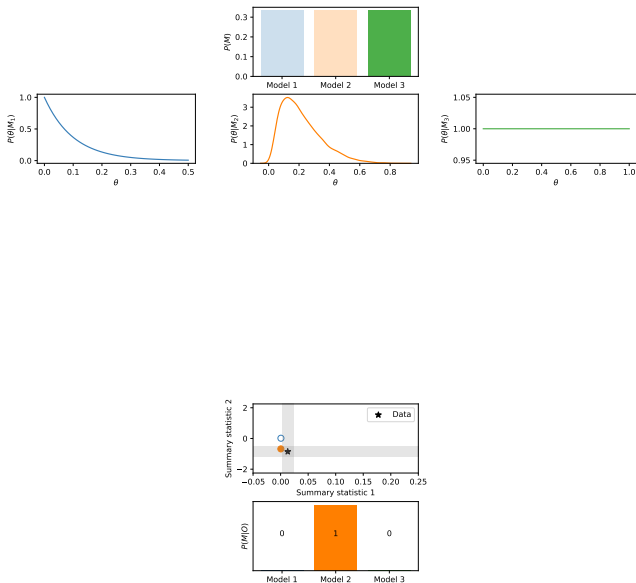
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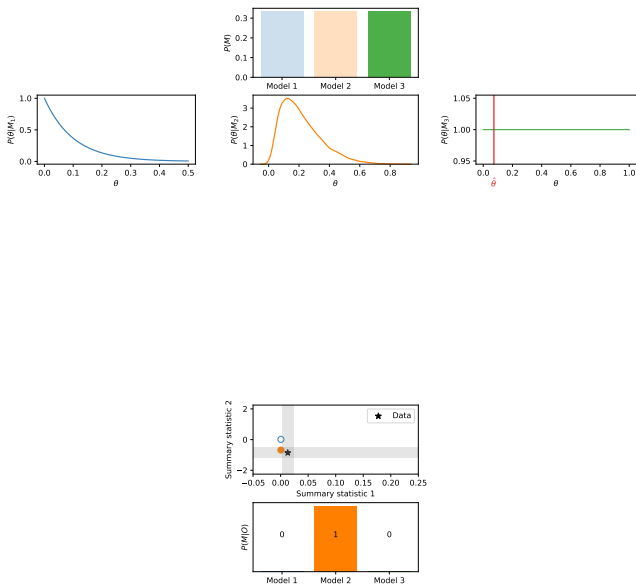
Simulation-based inference with summary statistics



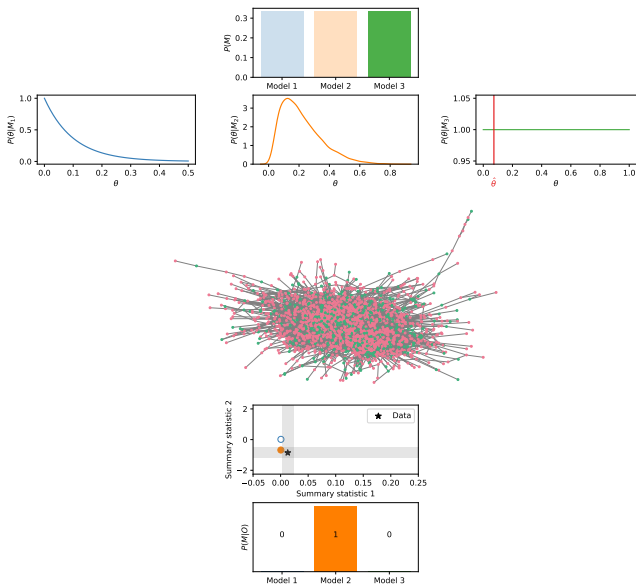
Simulation-based inference with summary statistics



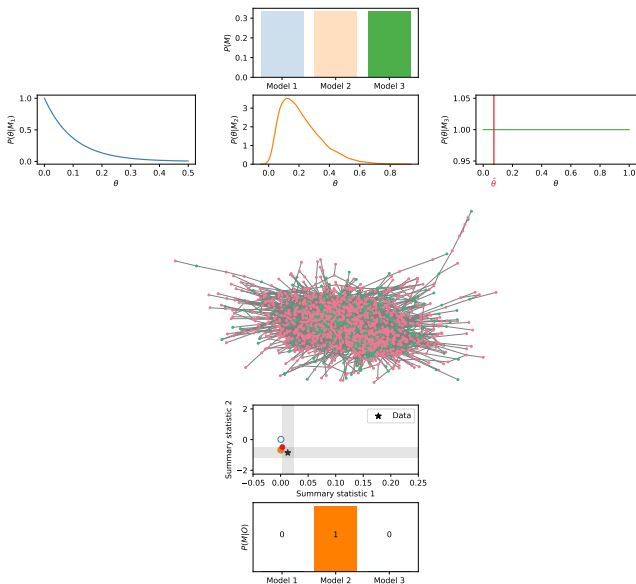
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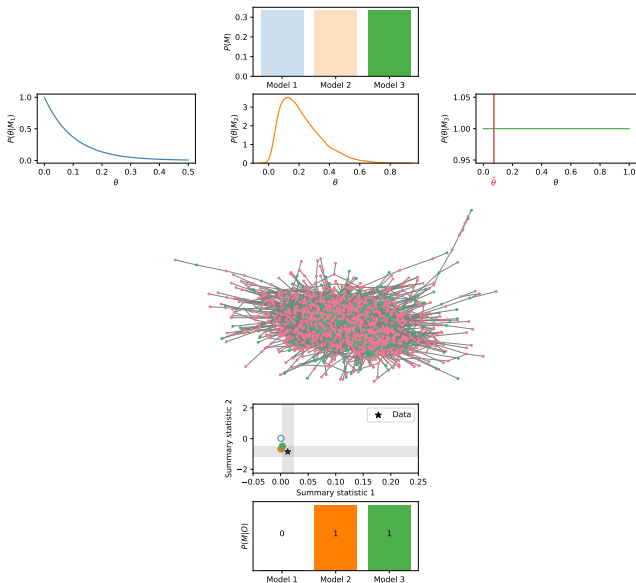
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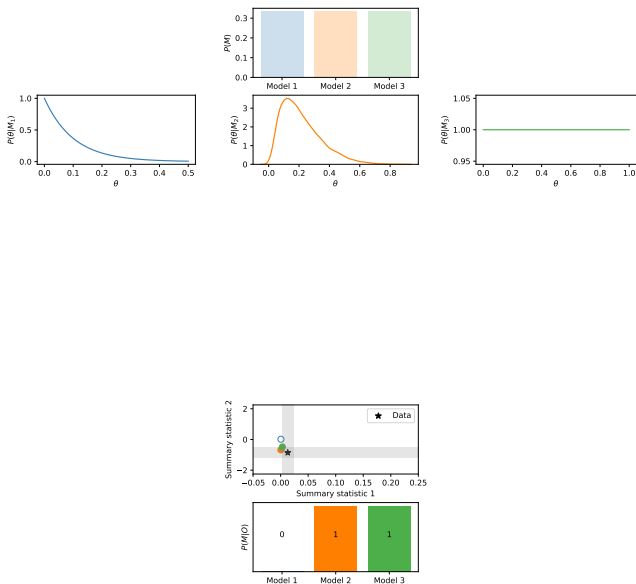
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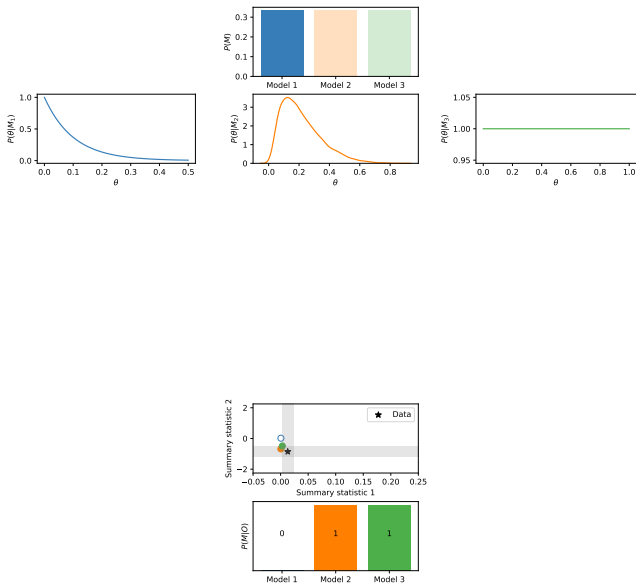
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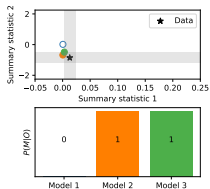
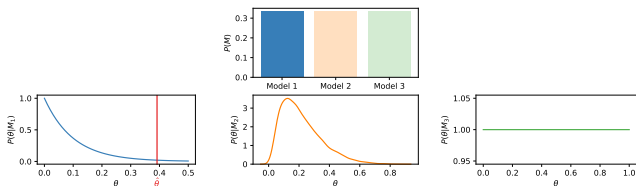
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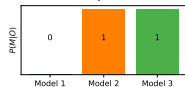
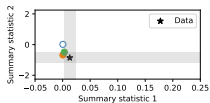
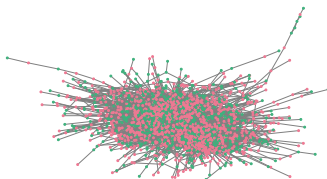
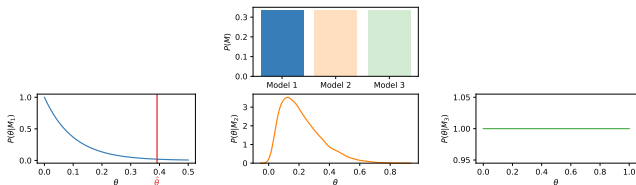
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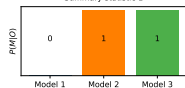
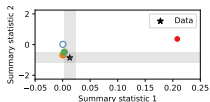
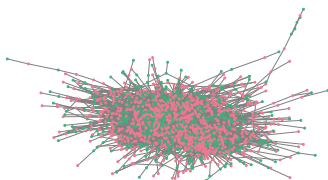
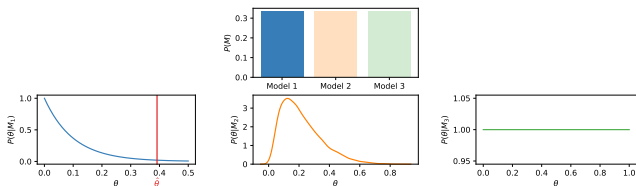
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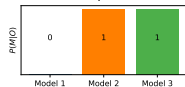
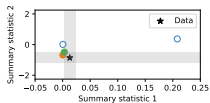
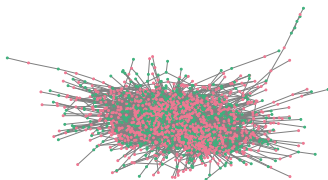
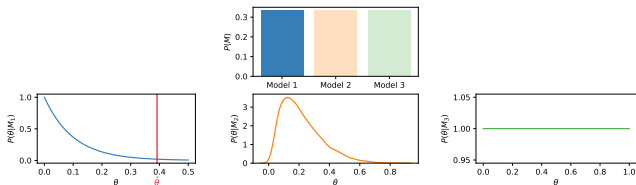
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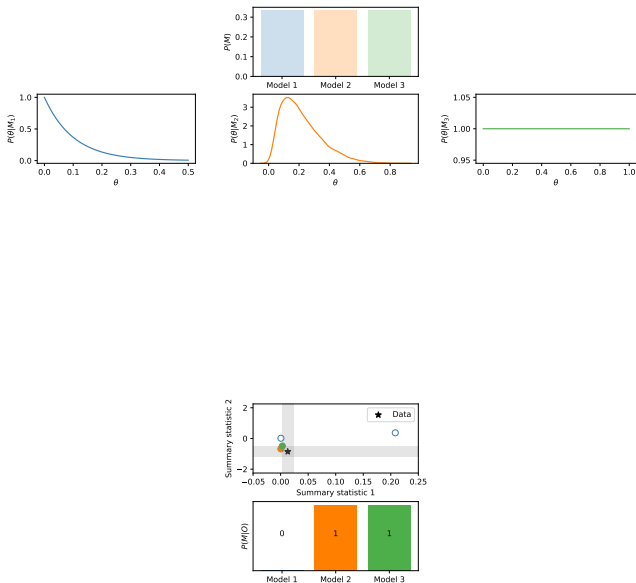
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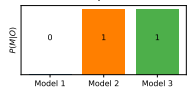
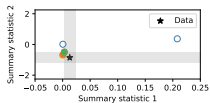
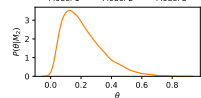
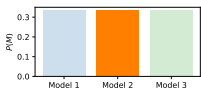
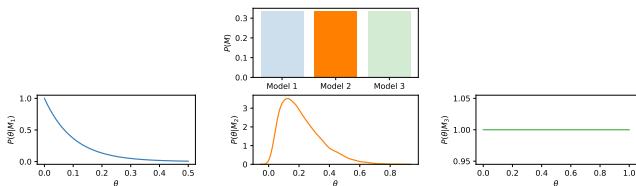
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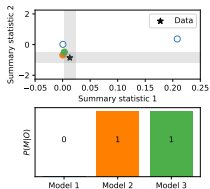
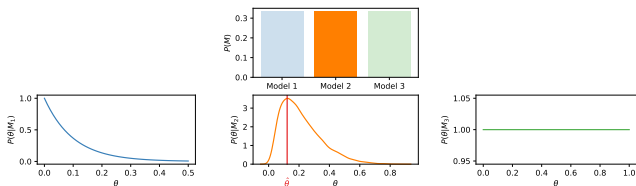
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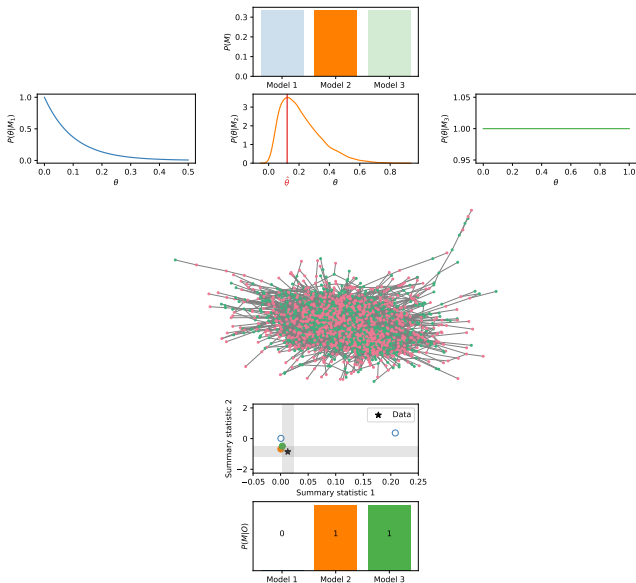
Simulation-based inference with summary statistics



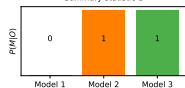
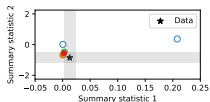
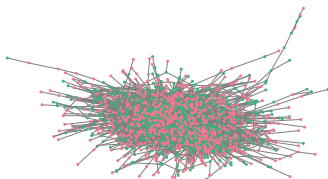
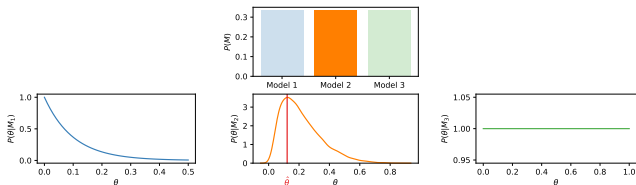
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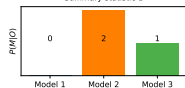
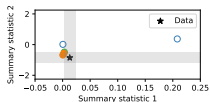
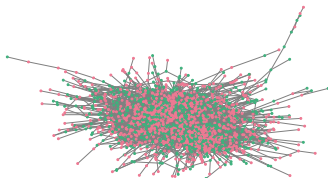
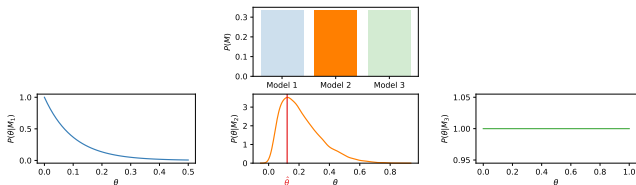
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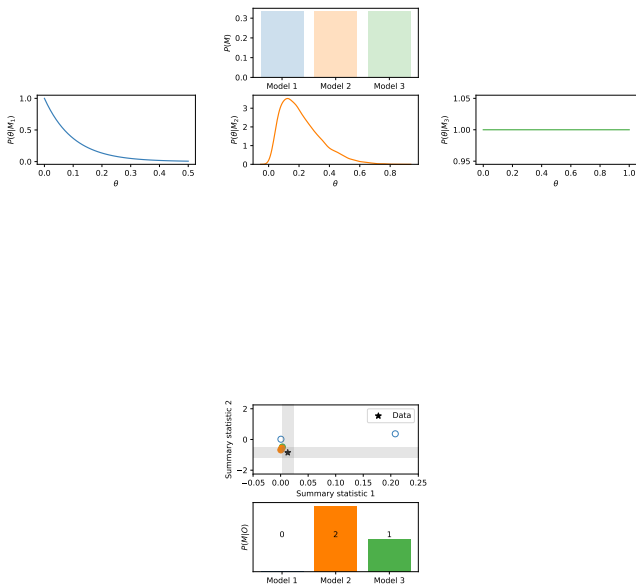
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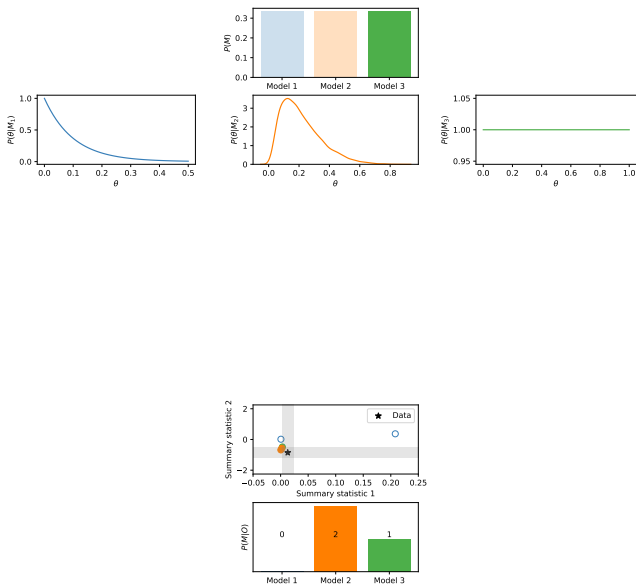
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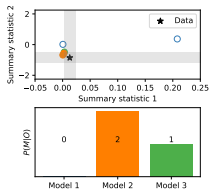
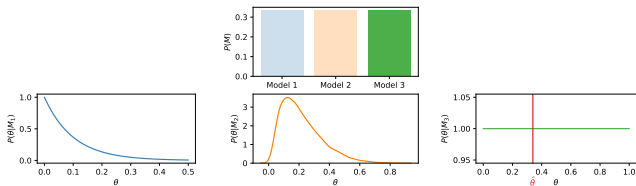
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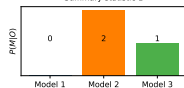
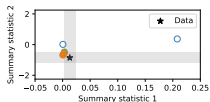
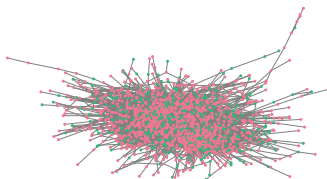
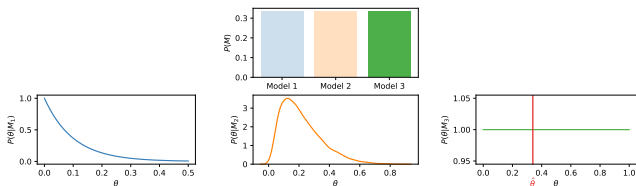
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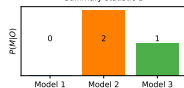
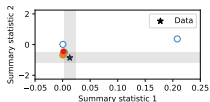
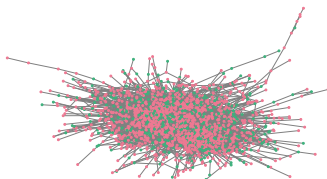
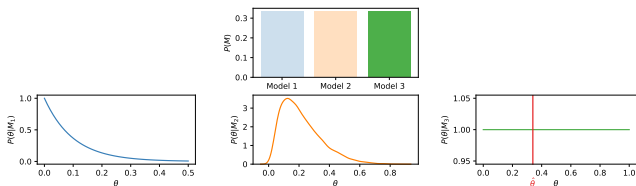
Simulation-based inference with summary statistics



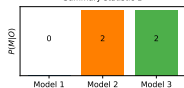
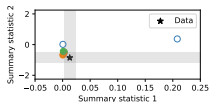
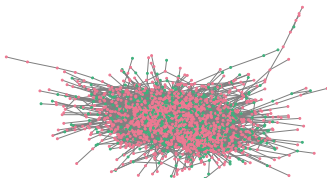
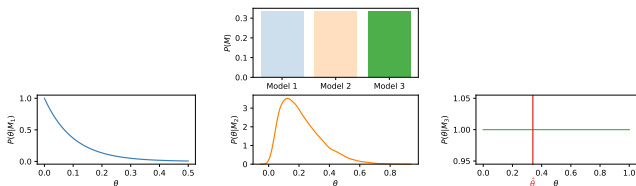
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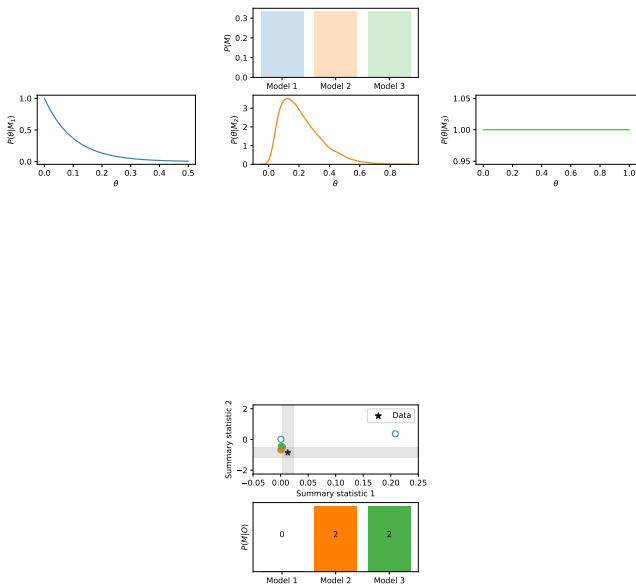
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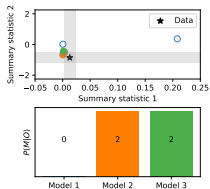
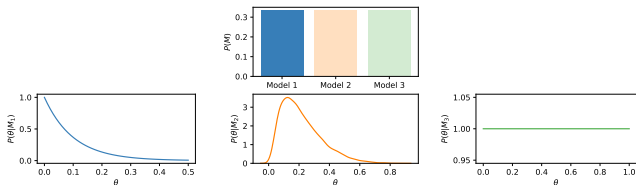
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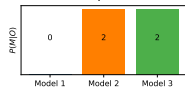
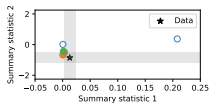
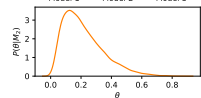
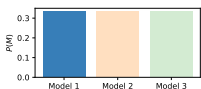
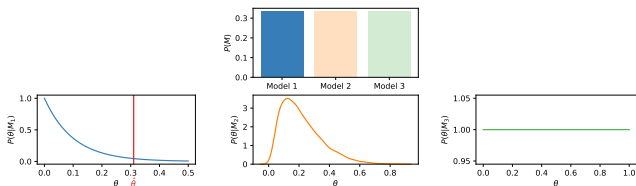
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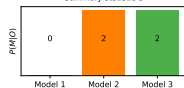
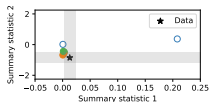
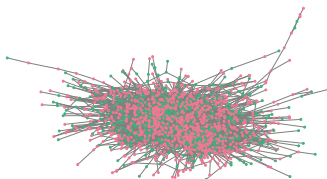
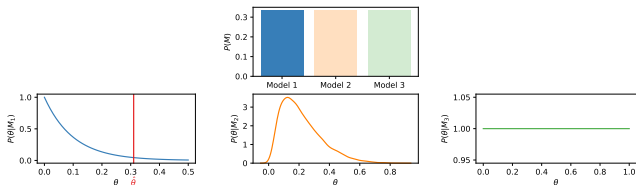
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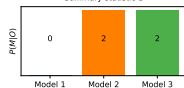
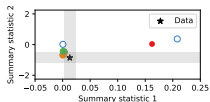
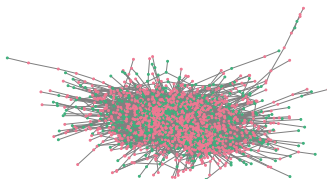
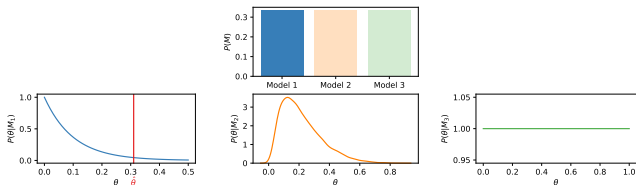
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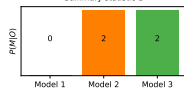
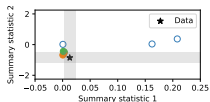
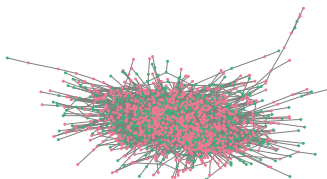
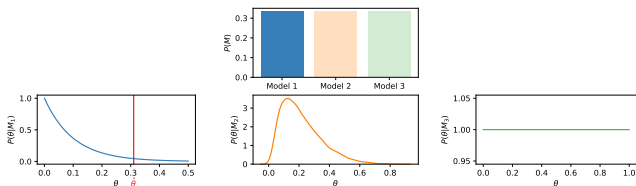
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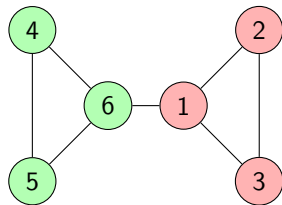
Simulation-based inference with summary statistics



Simulation-based inference with summary statistics



Local versus global mechanisms of coordination

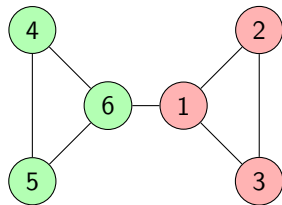


Local coordination

Strategic alignment,
imitation of peers...

J

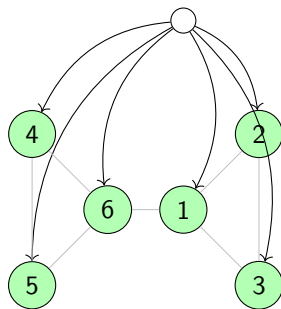
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Global coordination

Adaptation to research purposes,
or shared culture (“disciplinary matrix”)

B

The Ising model as an intermediate idealized model

- Atomic magnetic spins in a material can be in two states: $\uparrow (+1)$ or $\downarrow (-1)$.
- Magnetic spins prefer to be aligned to their neighbors ($\uparrow\uparrow$ or $\downarrow\downarrow$)
- Can local interactions between spins at the microscopic level lead to macroscopic alignment?

$$P(\{\sigma_i\} | J, \mathbf{B}) = \frac{1}{Z(J, \mathbf{B})} e^{-H(\{\sigma_i\}, J, \mathbf{B})}, \text{ and } H = - \underbrace{\sum_{i,j} J w_{ij} \sigma_i \sigma_j}_{\text{local pairwise interactions}} - \underbrace{\sum_i B_{C_i} \sigma_i}_{\text{external magnetic field}} \quad (6)$$

<https://mattbierbaum.github.io/ising.js/>

Inverse Ising problem: $P(J, J^{\text{cit}}, \mathbf{B} | \{\sigma_i\})$

Local coordination in multi-layered graphs

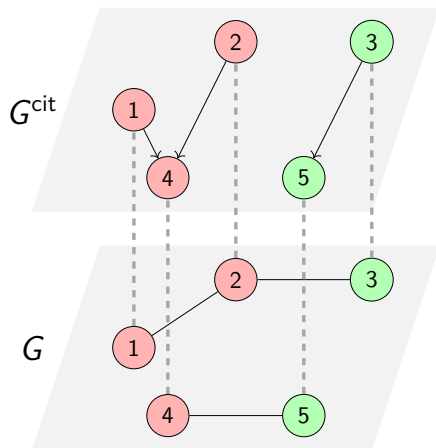


Figure: Illustration of local coordination in multilayered social networks. Nodes can be connected through different kinds of relationships (for instance, authors can be related via collaborations (G) or citations (G^{cit})).

Local versus global coordination

Table: Parameters of the Ising model.

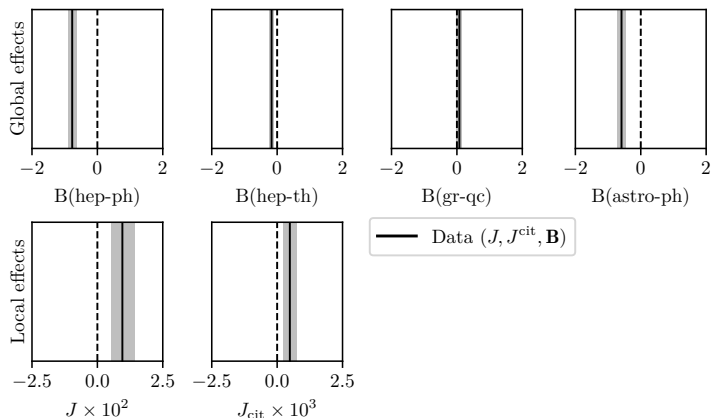
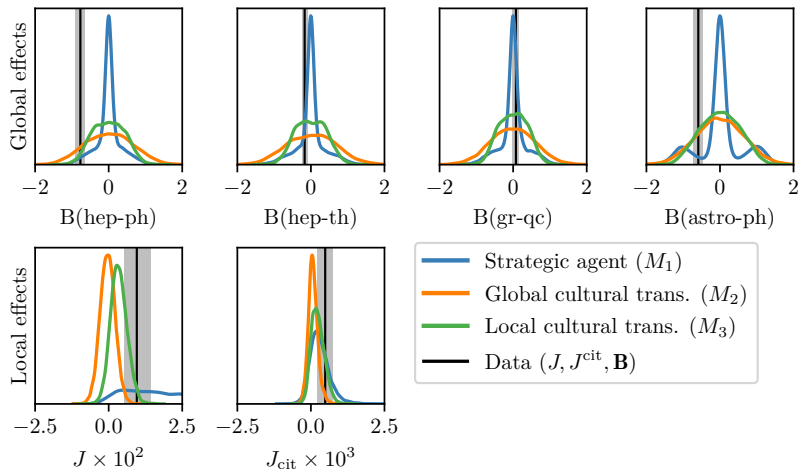


Figure: Ising model fit

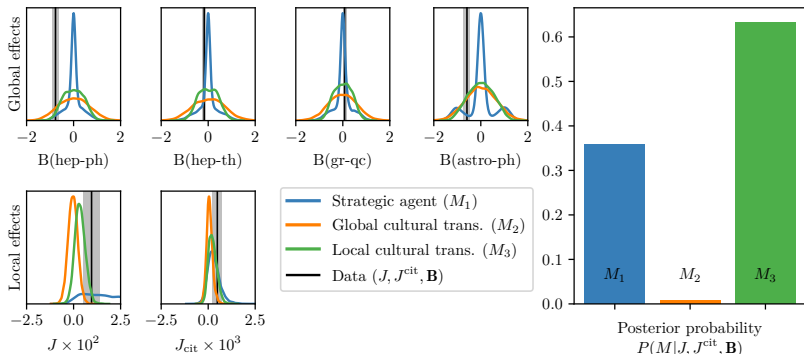
Local versus global coordination

What values of \mathbf{J} and \mathbf{B} do our models predict? In other words, what is the probability $P(\mathbf{J}, J^{\text{cit}}, \mathbf{B} | M_i)$ for each model M_i ?



Local versus global coordination

Given $P(\mathbf{J}, \mathbf{J}^{\text{cit}}, \mathbf{B} | M_i)$, and the true values of \mathbf{J} and \mathbf{B} , what is $P(M_i | \mathbf{J}, \mathbf{J}^{\text{cit}}, \mathbf{B})$?
After a bit of computational trickery – “amortized simulation-based model comparison with neural networks” with BayesFlow –:



Challenges for model selection

- Model misspecification: model comparison among highly incorrect models is challenging/meaningless

Challenges for model selection

- Model misspecification: model comparison among highly incorrect models is challenging/meaningless
- Priors on models' parameter matter. A model is disadvantaged if it only is a good fit to the data for improbable parameter values.

Summary: inverse problems in practice

- 1 What **phenomenon**? (Belief-polarization? Discrimination and marginalization? etc.)
- 2 What **models**? (“model-space”)
- 3 What **data**?
 - Accessibility (reasonable time/financial cost)
 - Quality (bias? ecological validity?)
 - Quantity (statistical significance)
- 4 What **computational strategies**?
 - **Pre-processing**: e.g. text-classification (natural language processing)?
 - **Inference** (inverse problem): simulation-based inference (with/without neural networks); Hamiltonian Monte-Carlo? Metropolis?

Thank you! I



Centola, Damon and Andrea Baronchelli (Feb. 2015). “The spontaneous emergence of conventions: An experimental study of cultural evolution”. In: *Proceedings of the National Academy of Sciences* 112.7.



Cranmer, Kyle, Johann Brehmer, and Gilles Louppe (May 2020). “The frontier of simulation-based inference”. In: *Proceedings of the National Academy of Sciences* 117.48.



Delgado, Jordi (2002). “Emergence of social conventions in complex networks”. In: *Artificial intelligence* 141.1-2.



Hawkins, Robert XD, Noah D Goodman, and Robert L Goldstone (2019). “The emergence of social norms and conventions”. In: *Trends in cognitive sciences* 23.2.



Lewis, David (Jan. 1969). *Convention: A Philosophical Study*. Cambridge, MA: Harvard University Press.



O’Connor, Cailin (June 2020). “Measuring Conventionality”. In: *Australasian Journal of Philosophy* 99.3.



Pujol, Josep M et al. (2005). “The role of clustering on the emergence of efficient social conventions”. In: *Proceedings of the 19th international joint conference on Artificial intelligence*.



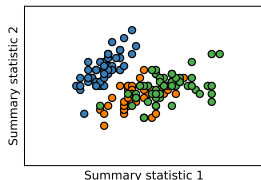
Radev, Stefan T et al. (2021). “Amortized bayesian model comparison with evidential deep learning”. In: *IEEE Transactions on Neural Networks and Learning Systems* 34.8.

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 - Use amortized inference with neural networks \Rightarrow train a neuralnet to predict the probability of each model M_i given one or more observed outcomes. The neuralnet is trained with many simulated training samples (M_s, O_s) (Radev et al., 2021)

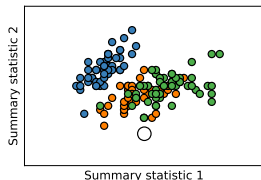
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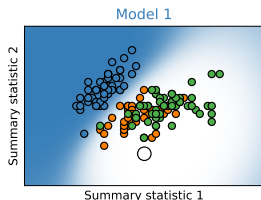
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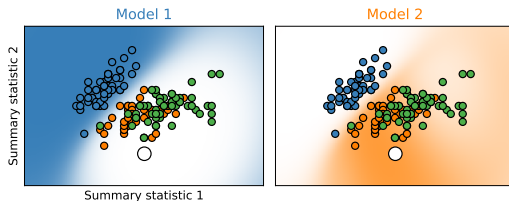
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